

# SLAC's Test Bed for Superconducting Materials: System Description and Preliminary Results

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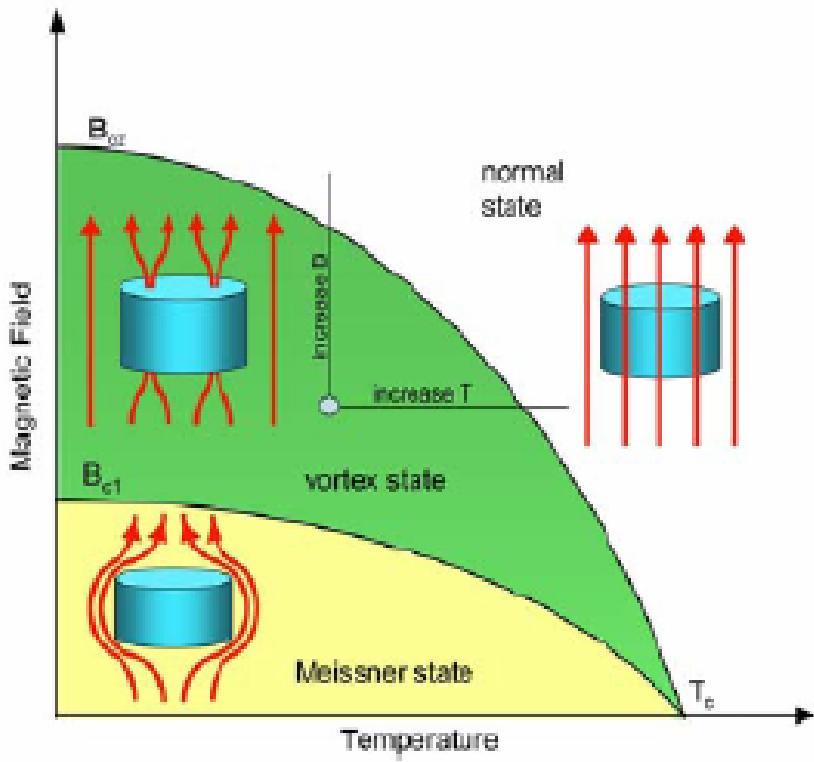
UNCLASSIFIED

# Contents

- Overview
  - Superconducting RF (SRF)
  - System Description
  - Results
- Cavity Model
  - Pulse Dependence
  - Critical Magnetic Field
- Results vs Model
  - Discussion and Future Tests

# Overview: SRF

- Magnetic critical fields



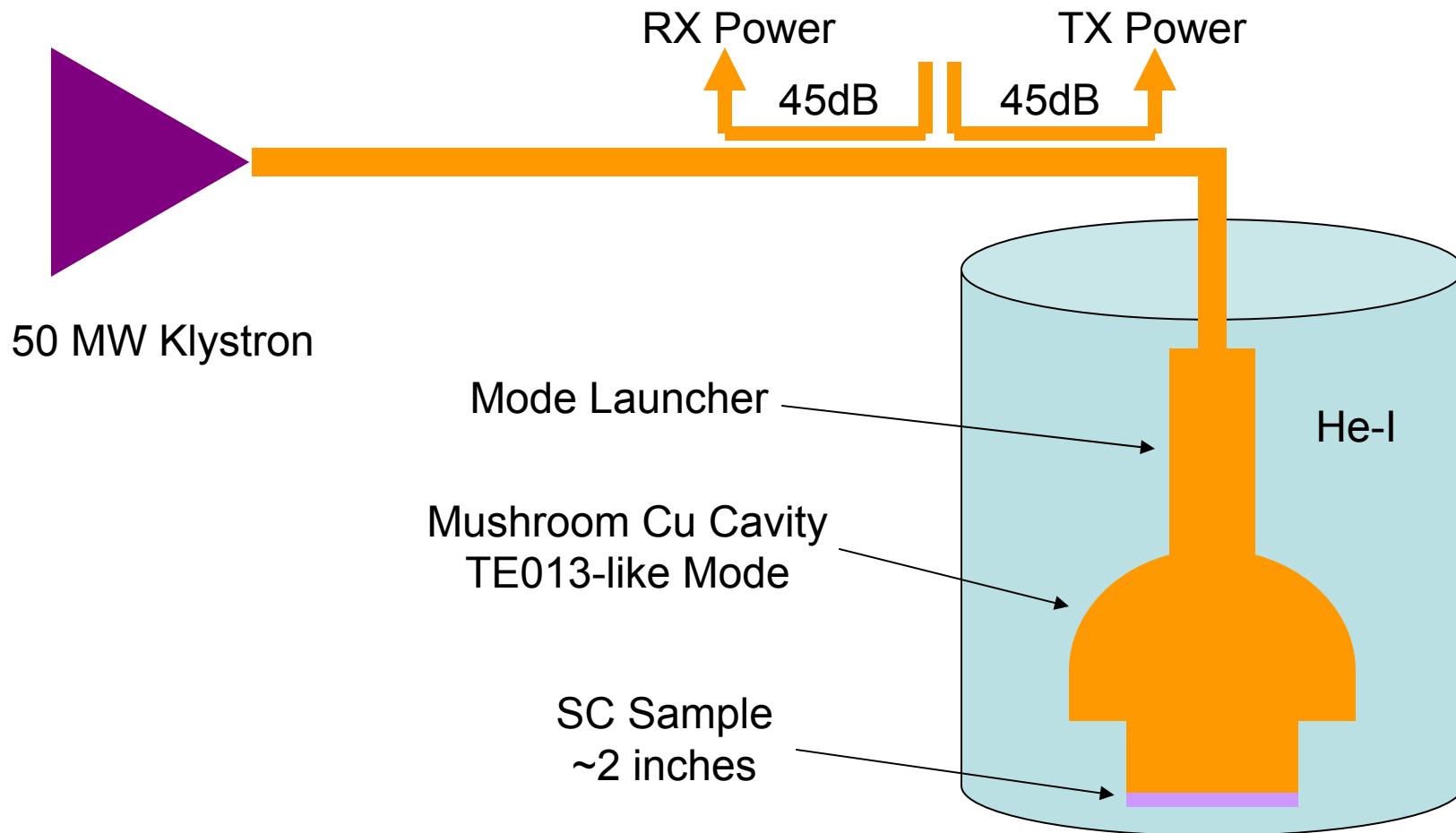
$$H_{c1} = \frac{\phi_0}{4\pi\mu\lambda_L^2} \left( \ln \frac{\lambda_L}{\xi} + 0.5 \right)$$

$$H_{c2} = \frac{\phi_0}{2\pi\mu\xi^2}$$

$$H_c = \frac{\phi_0}{2\sqrt{2}\pi\lambda_L\xi}$$

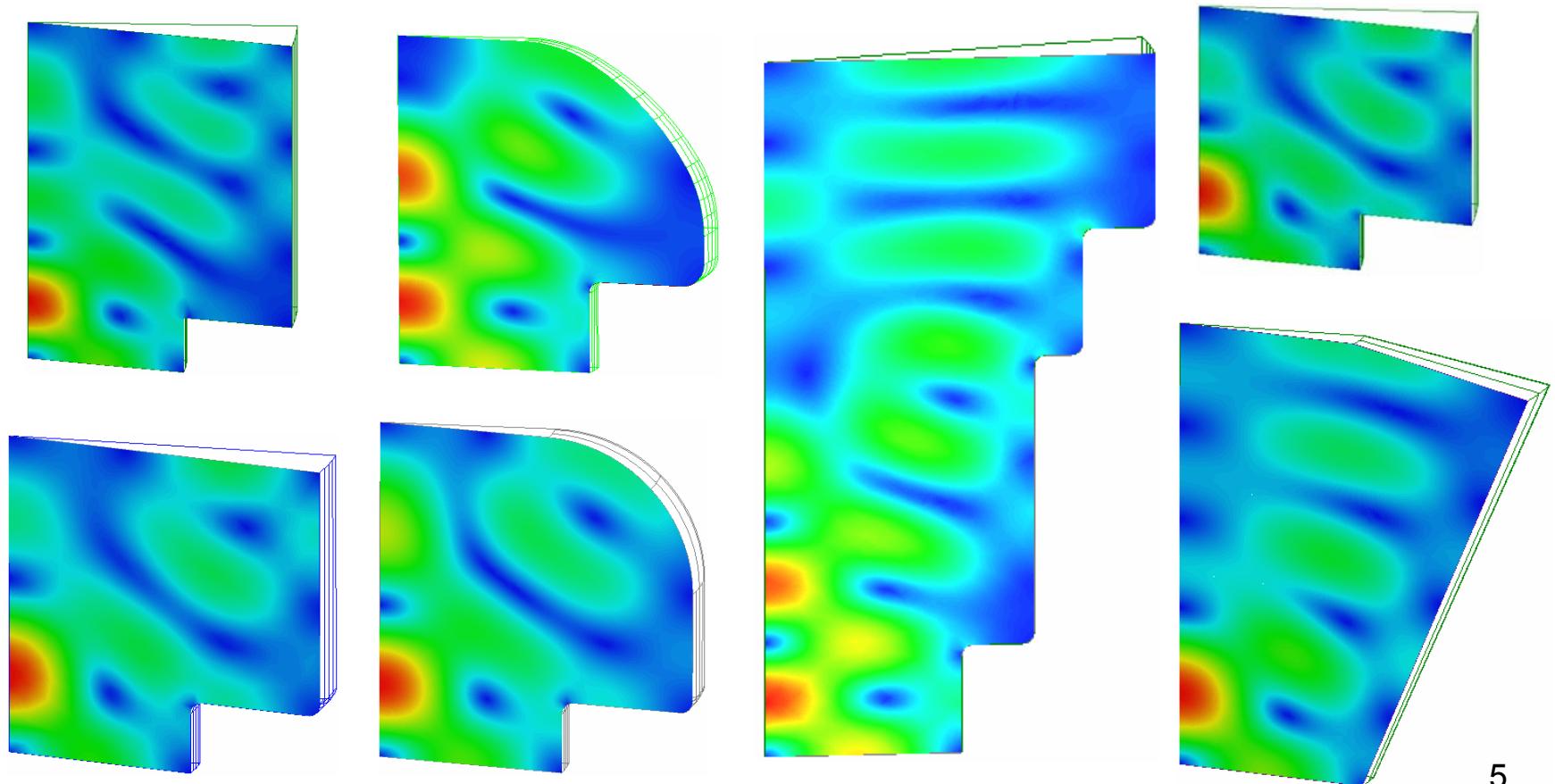
$$H_c^{RF} = ????$$

# Overview: System Description



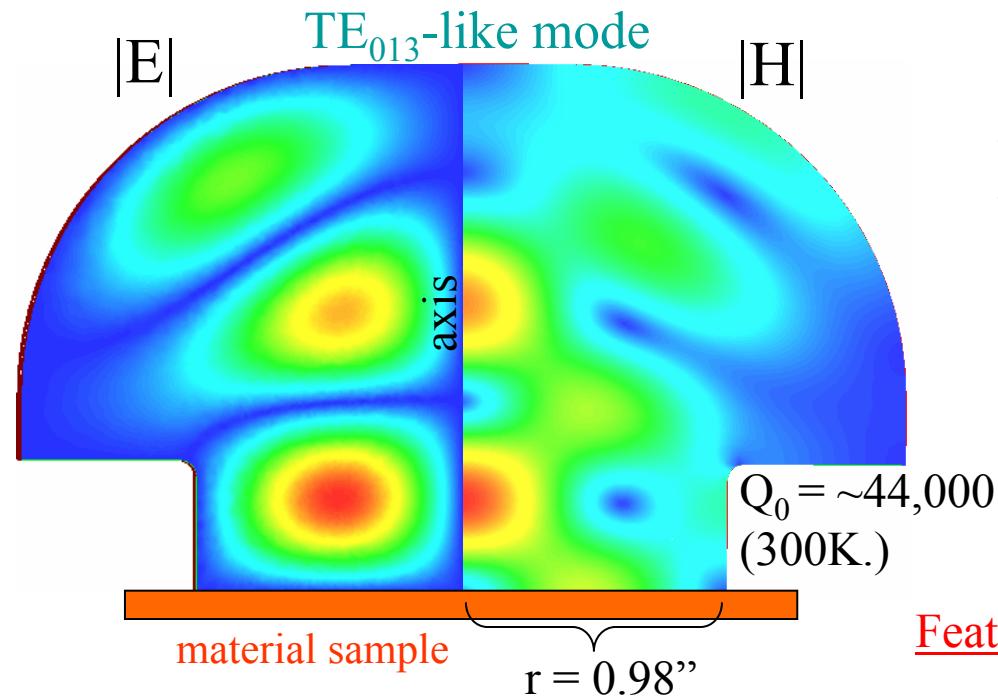
# Overview: System Description

- Cavity shape
  - TE01n pillbox (same field on top and bottom)



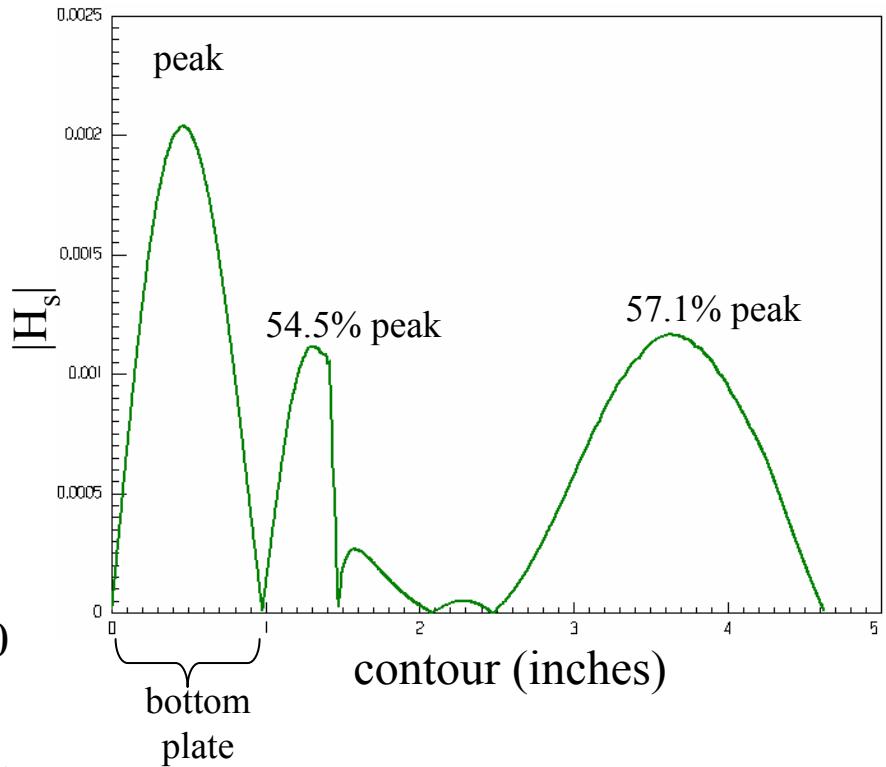
# Overview: System Description

- Mushroom cavity



Why X-band (~11.424 GHz)?:

- High power & RF components available
- Fits in cryogenic Dewar
- Small (3") samples required

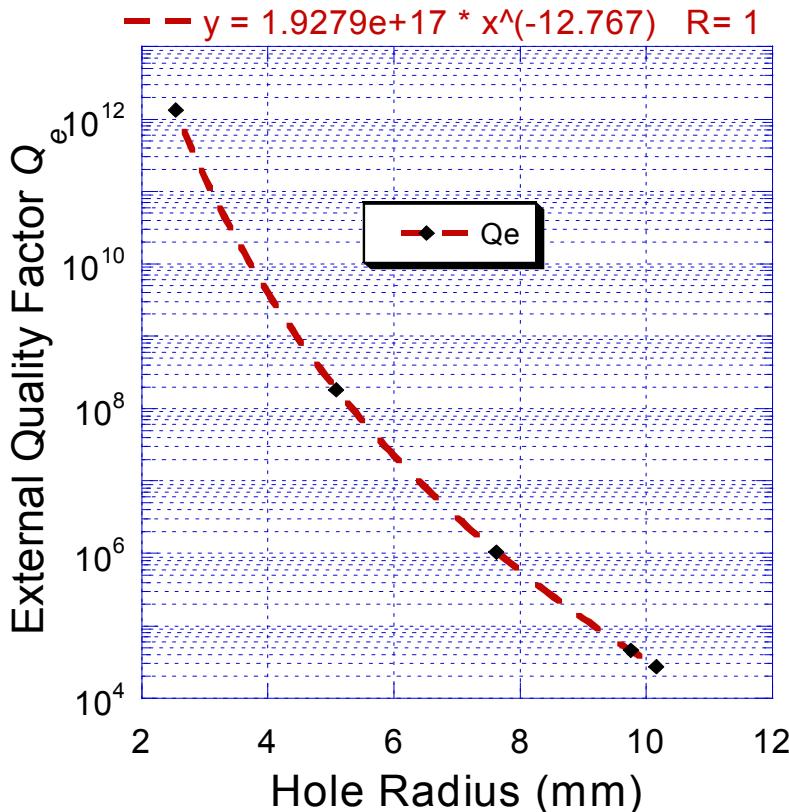


## Features:

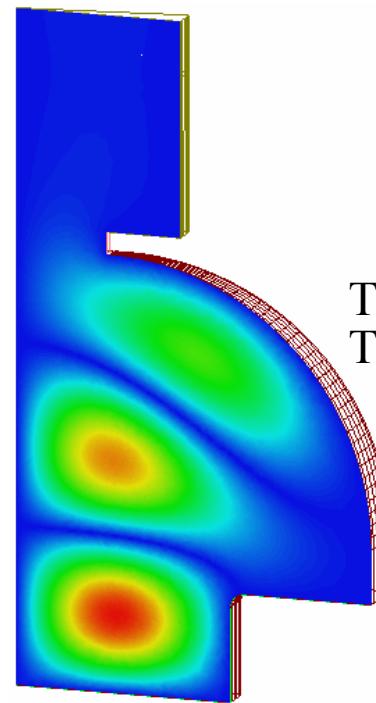
- No surface electric fields (no multipactor)
- Magnetic field concentrated on bottom (sample) face (75% higher than anywhere else)
- Purely azimuthal currents allow demountable bottom face (gap).<sup>6</sup>

# Overview: System Description

- Other nearby resonant modes
  - Couple on axis with pure axisymmetric transverse electric mode TE01 in circular waveguide.



WC150  
(3.81 cm diam.)



6.8% mode separation for axisymm. TE modes.

| Frequency (GHz) |                               |
|-----------------|-------------------------------|
| Mode 1          | ( 9.45389e+000, 0.00000e+000) |
| Mode 2          | ( 1.14234e+001, 0.00000e+000) |
| Mode 3          | ( 1.22026e+001, 0.00000e+000) |

4.0% mode separation from axisymm. TM mode.

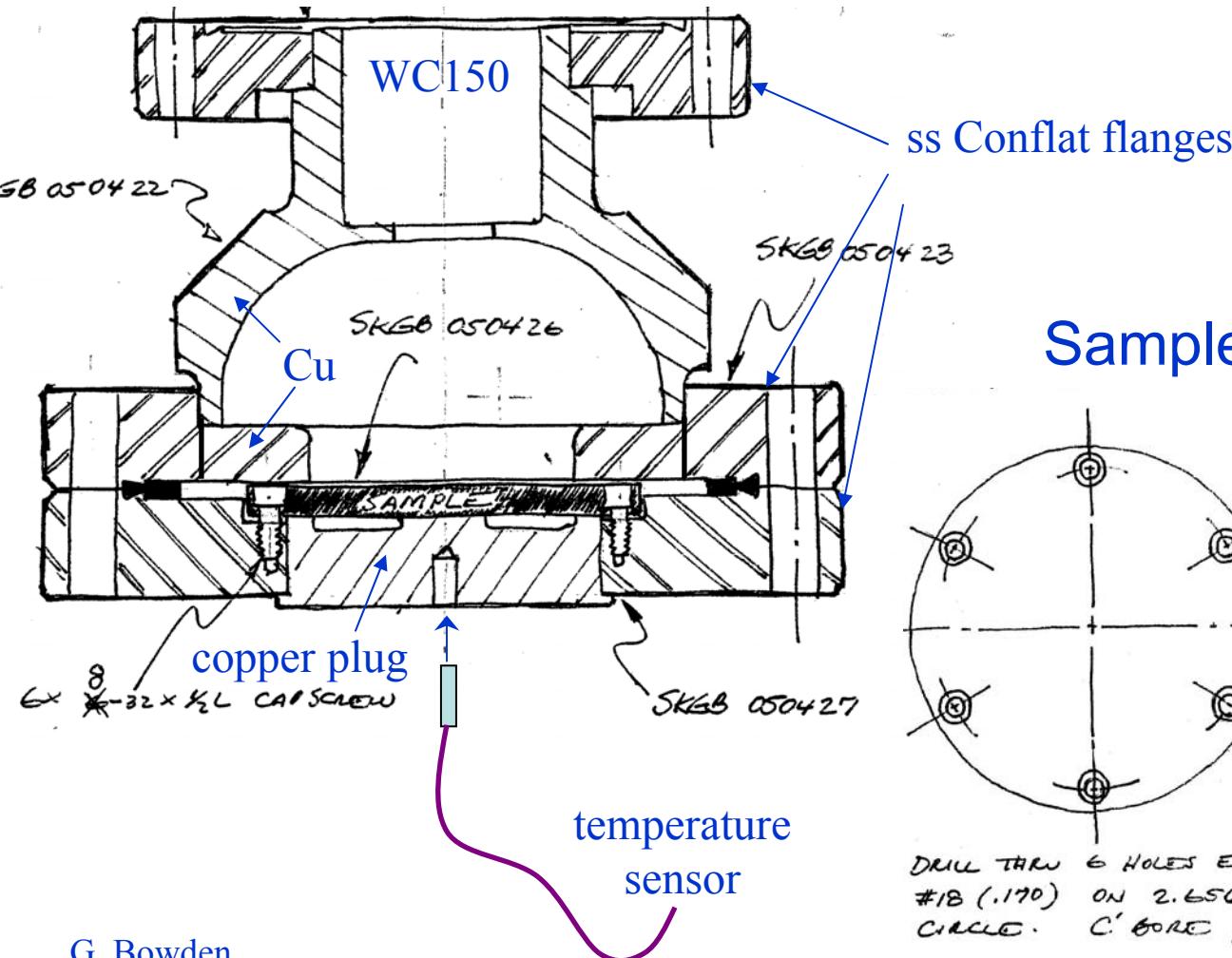
| Frequency (GHz) |                               |
|-----------------|-------------------------------|
| Mode 1          | ( 1.09513e+001, 0.00000e+000) |
| Mode 2          | ( 1.18826e+001, 0.00000e+000) |
| Mode 3          | ( 1.28660e+001, 0.00000e+000) |

1.4% mode separation from non-axisymm. mode.

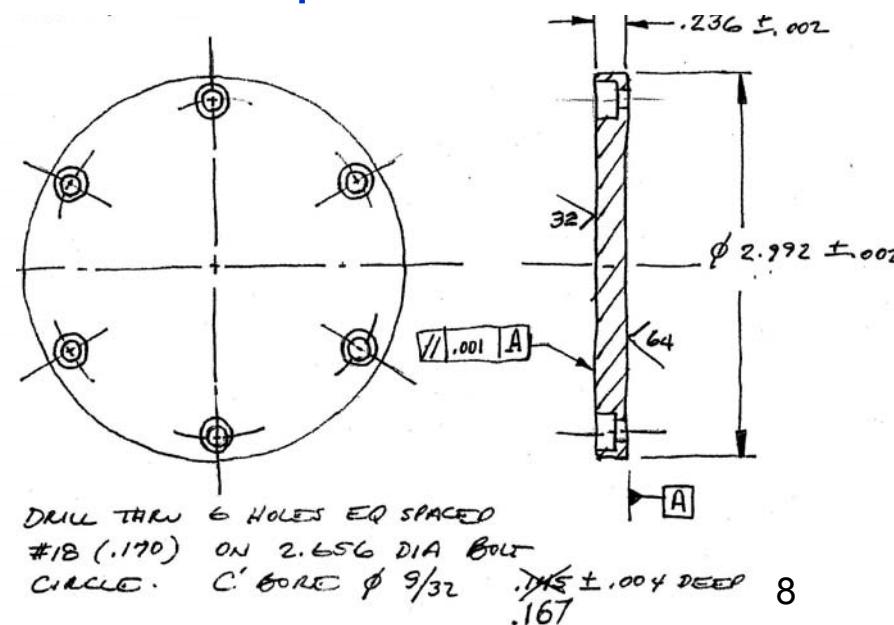
| Frequency (GHz)   |                               |
|-------------------|-------------------------------|
| TE <sub>131</sub> | ( 1.10167e+001, 0.00000e+000) |
| TM <sub>32?</sub> | ( 1.15877e+001, 0.00000e+000) |
| Mode 3            | ( 1.15983e+001, 0.00000e+000) |

# Overview: System Description

- Mechanical Design

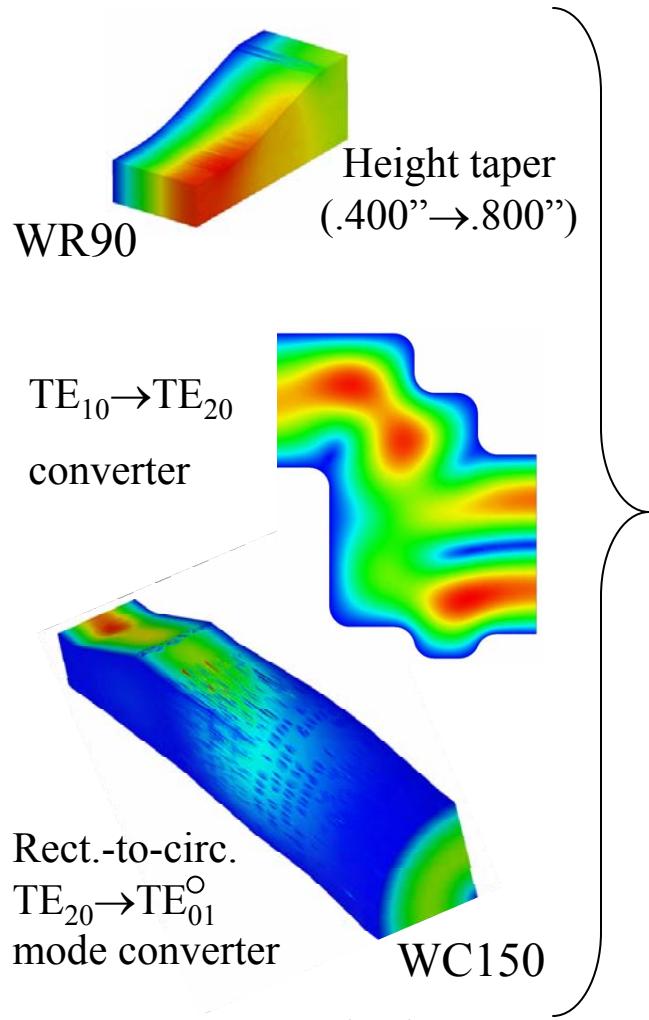


Sample Dimensions



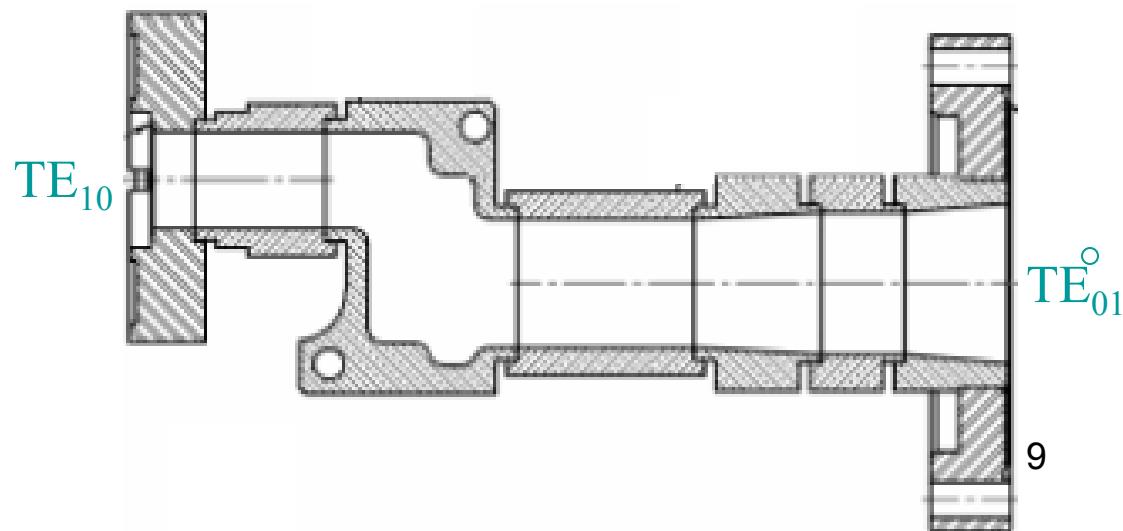
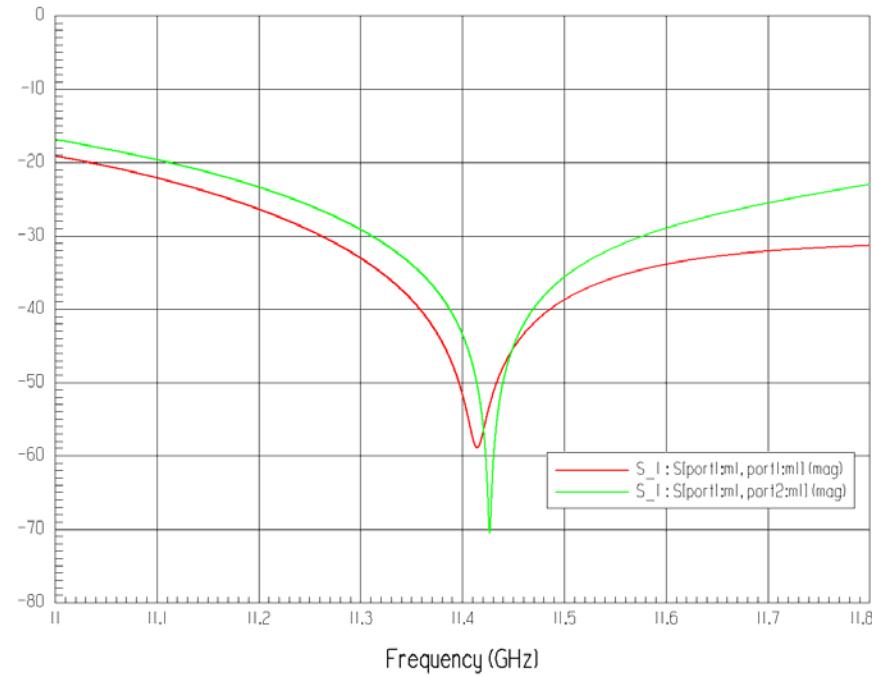
# Overview: System Description

- Mode launcher

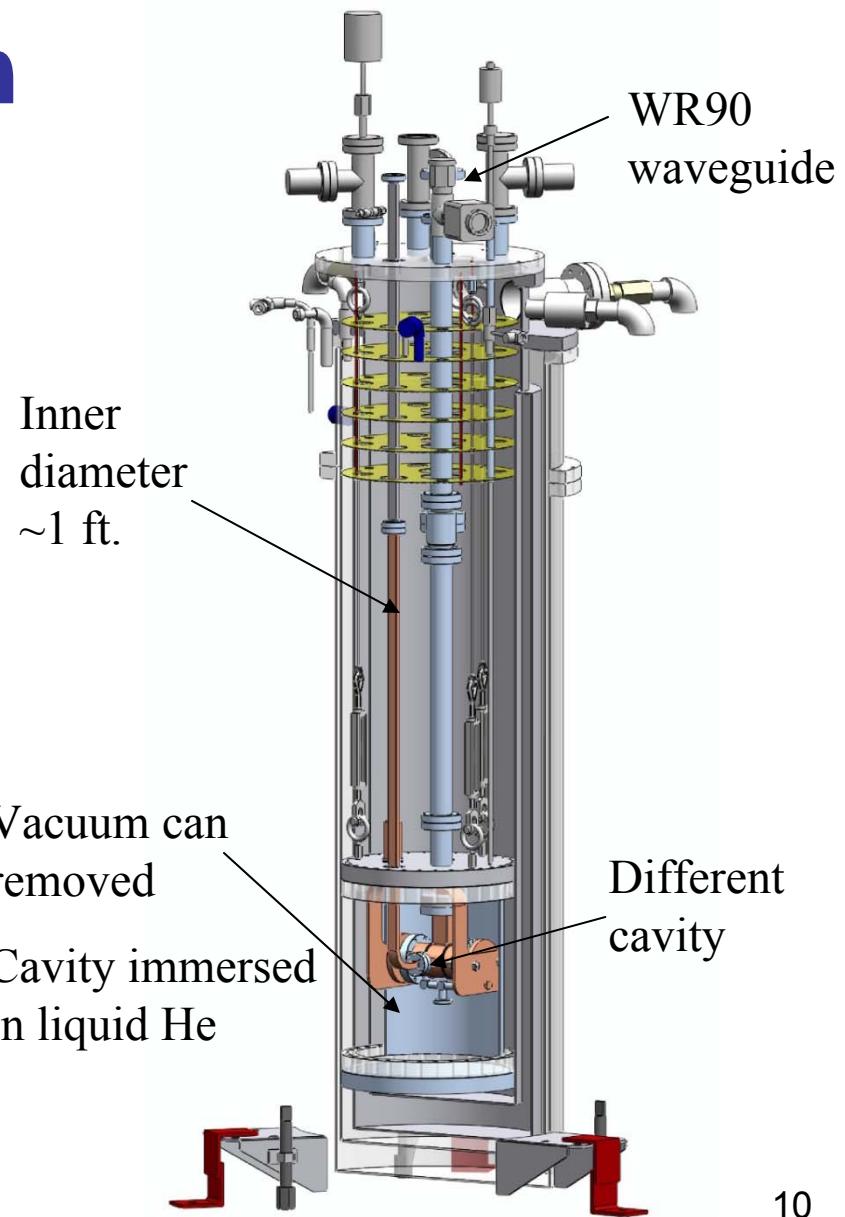
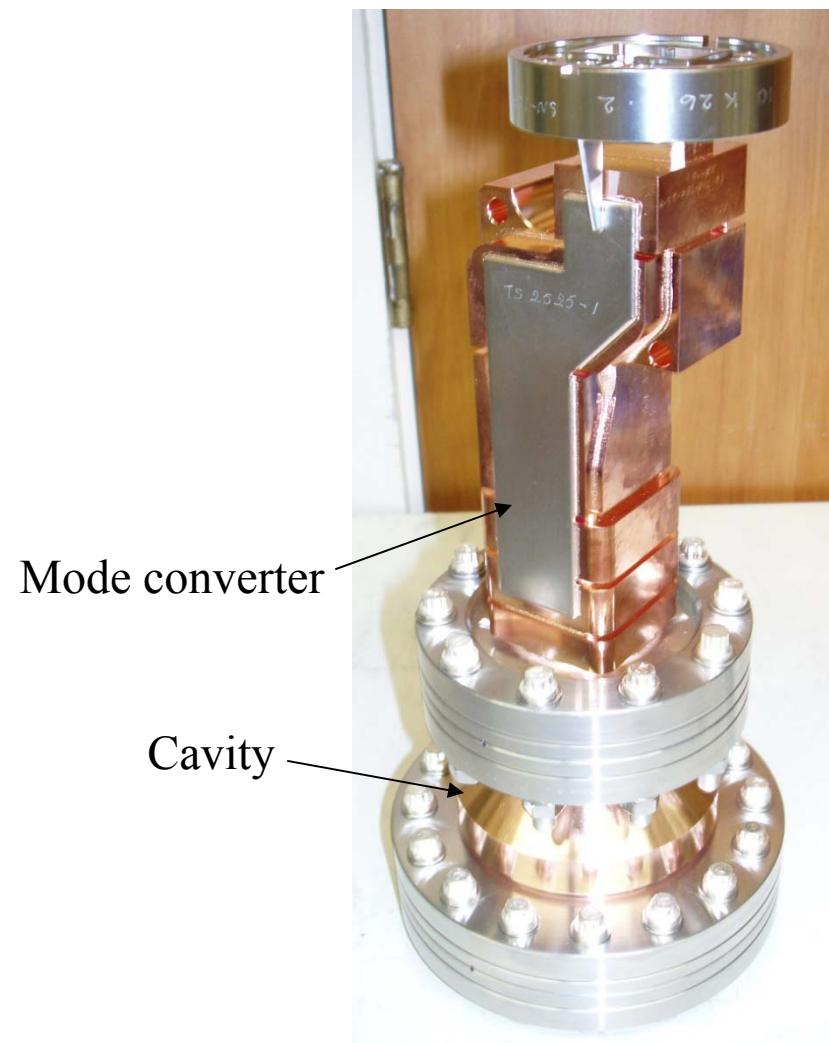


V. Dolgashev

WR90-WC150 Compact High-Purity  
TE01 Mode Launcher

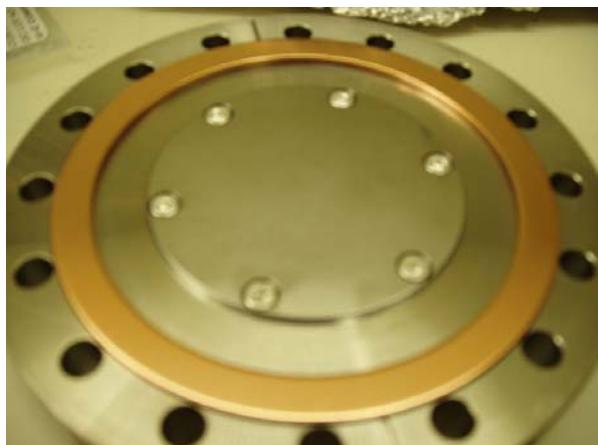


# Overview: System Description



# Overview: System Description

|         | HFSS (Cu) | Copper  | Niobium |
|---------|-----------|---------|---------|
| $f_r$   | 11.424    | 11.4072 | 11.4061 |
| $Q_L$   | 30,991    | 29,961  | 20,128  |
| $\beta$ | 0.4383    | 0.4611  | 0.2728  |
| $Q_0$   | 44,575    | 43,775  | 25,619  |
| $Q_e$   | 101,694   | 94,944  | 93,906  |



Nb sample mounted in bottom flange

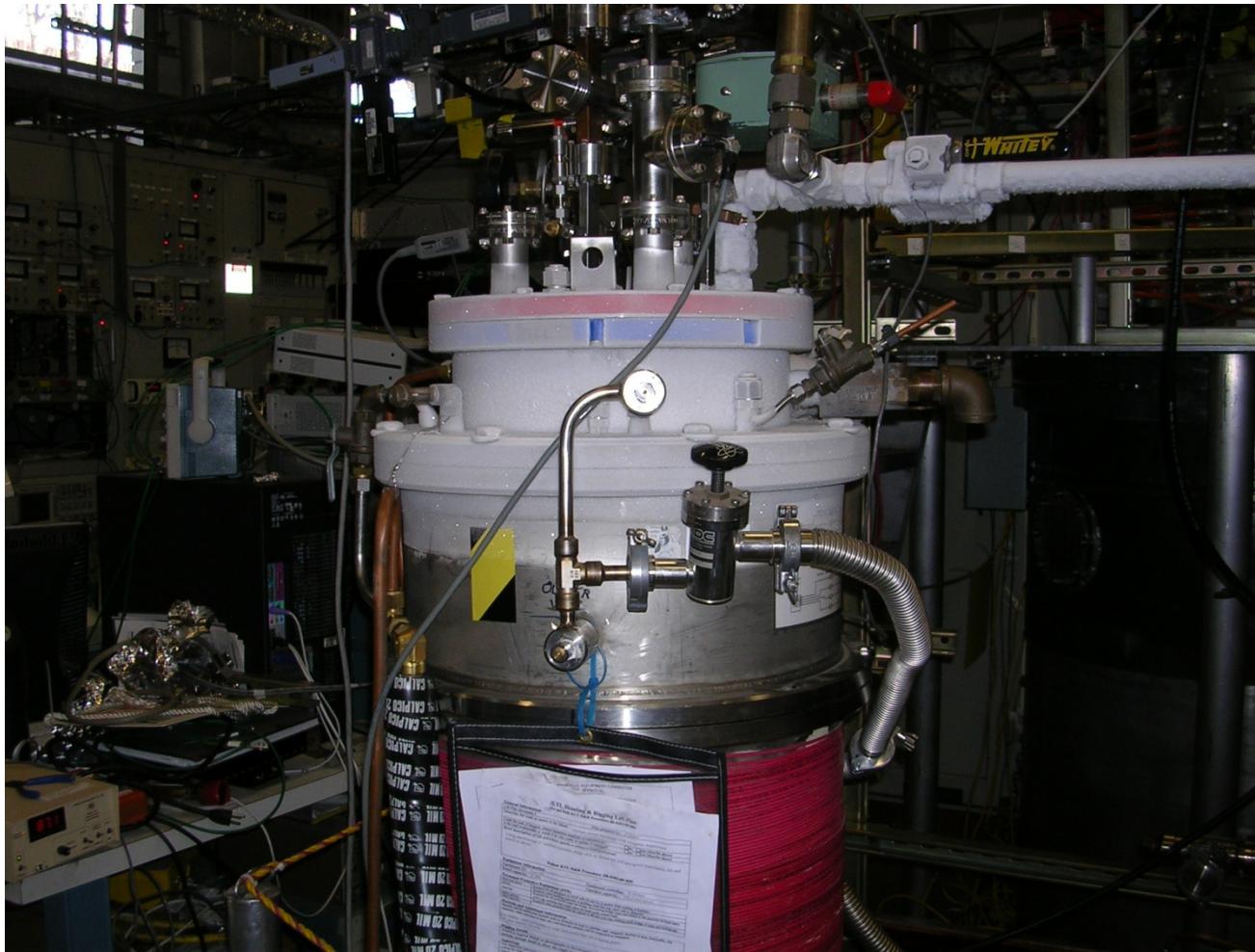
## Room Temperature Tests



HP 8510C Network Analyzer

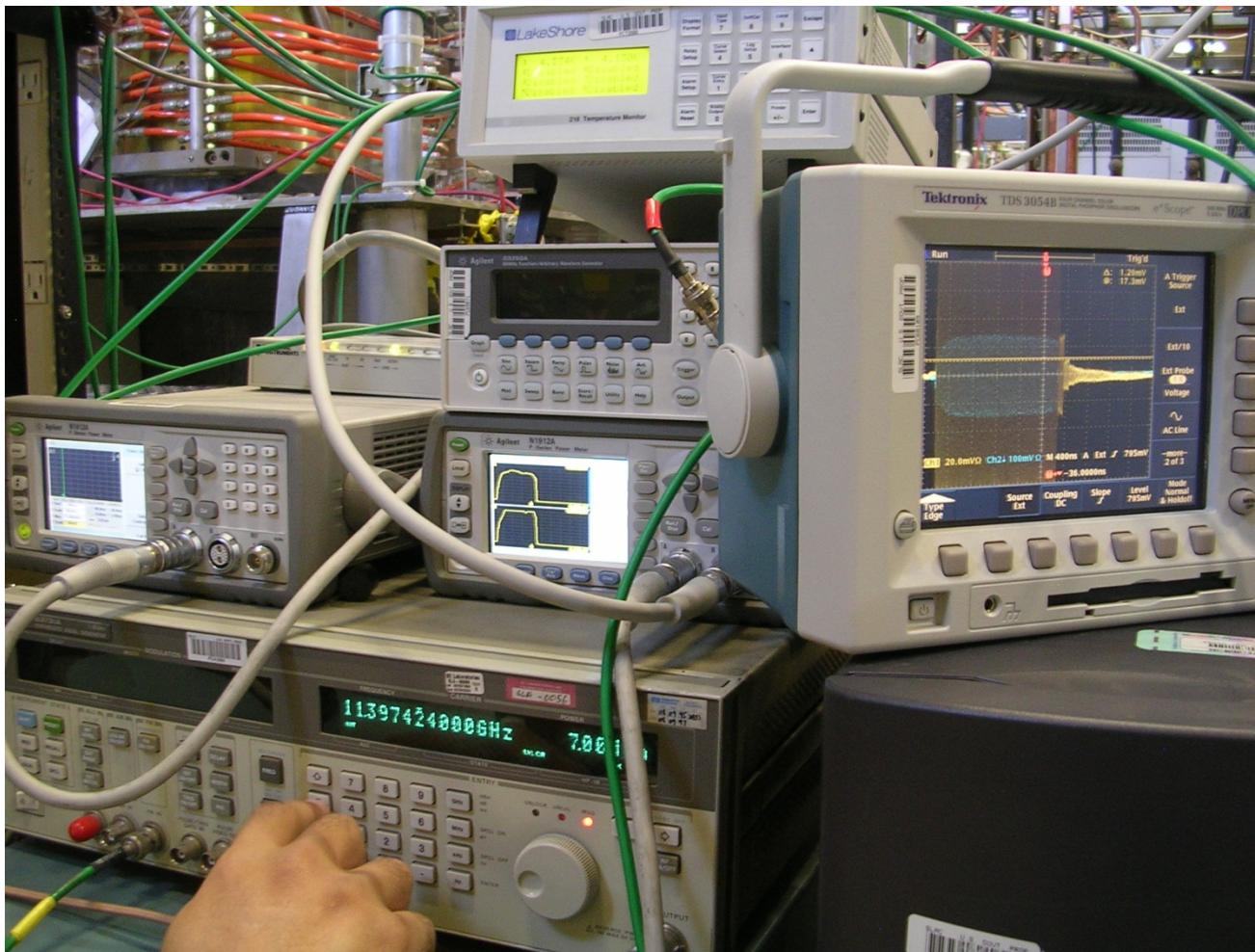
# Overview: System Description

- Photographs



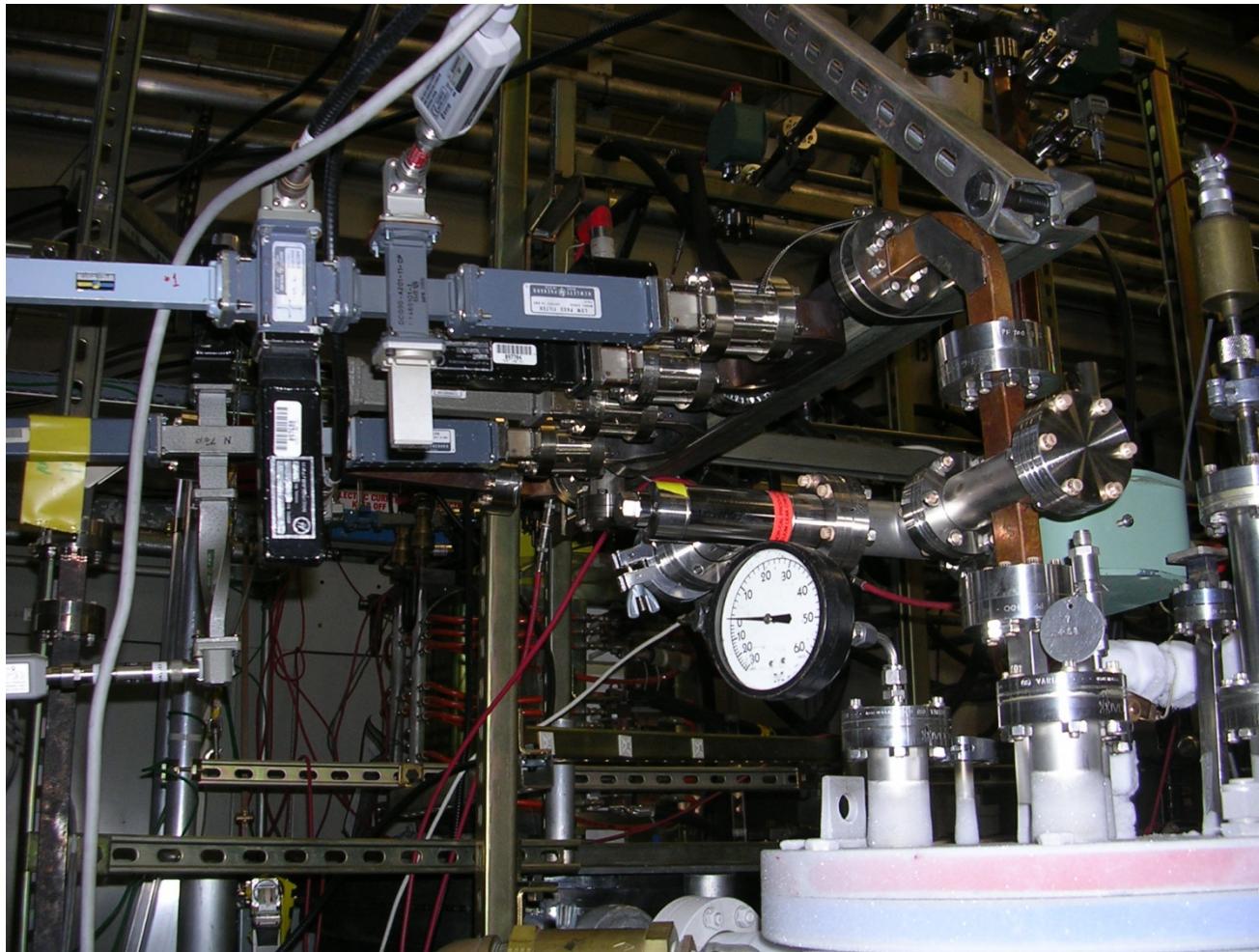
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## Photographs



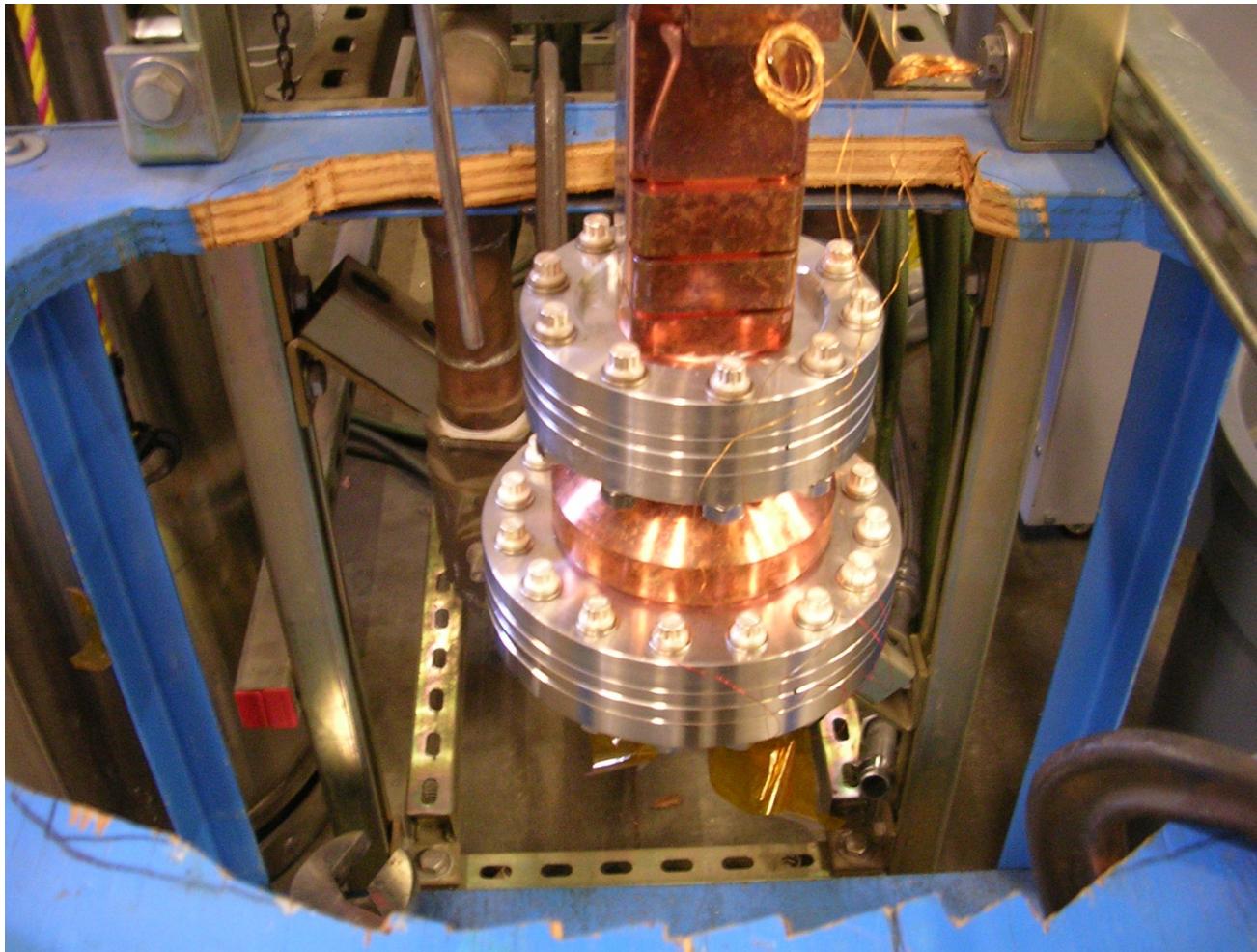
# Overview: System Description

## Photographs



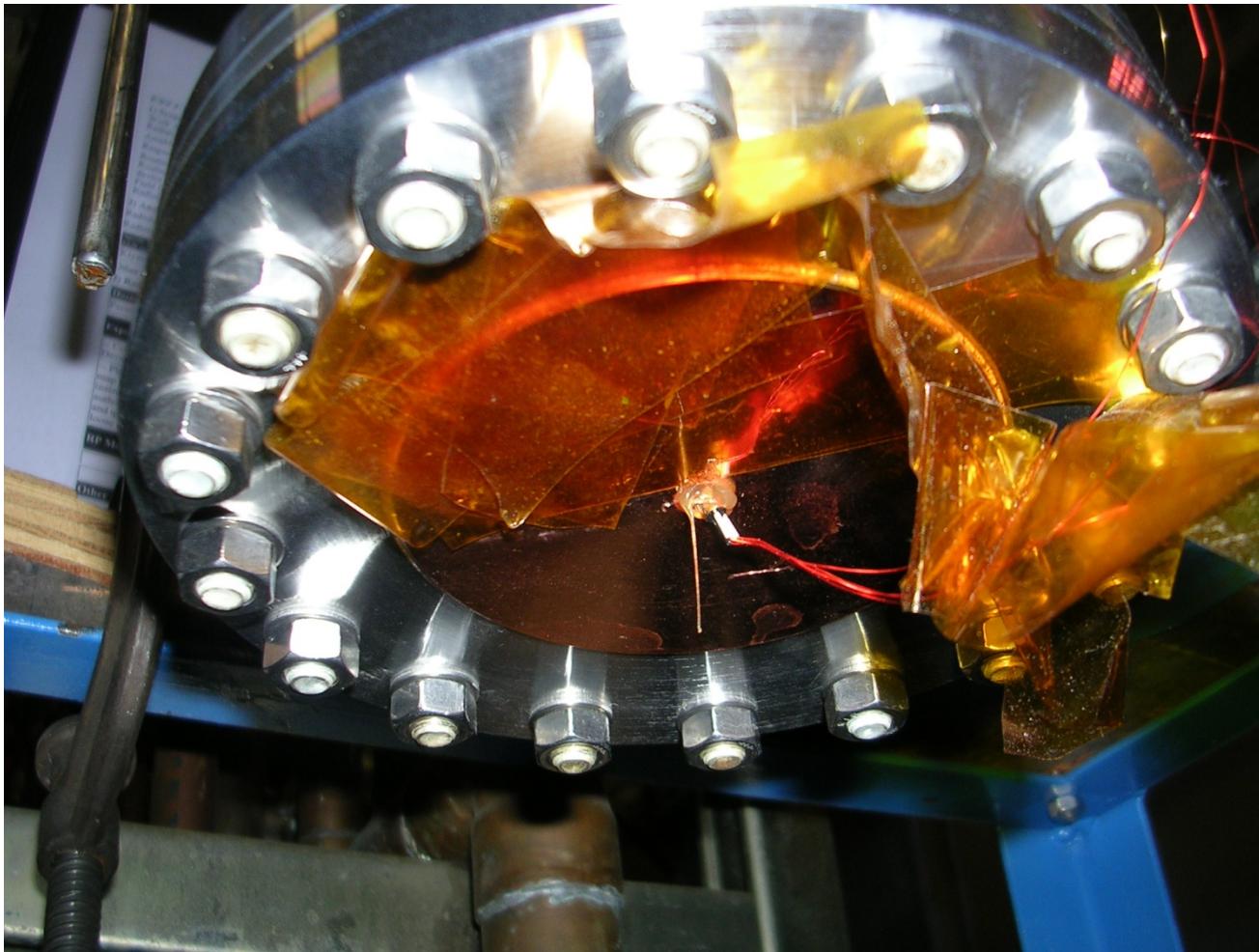
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## Photographs



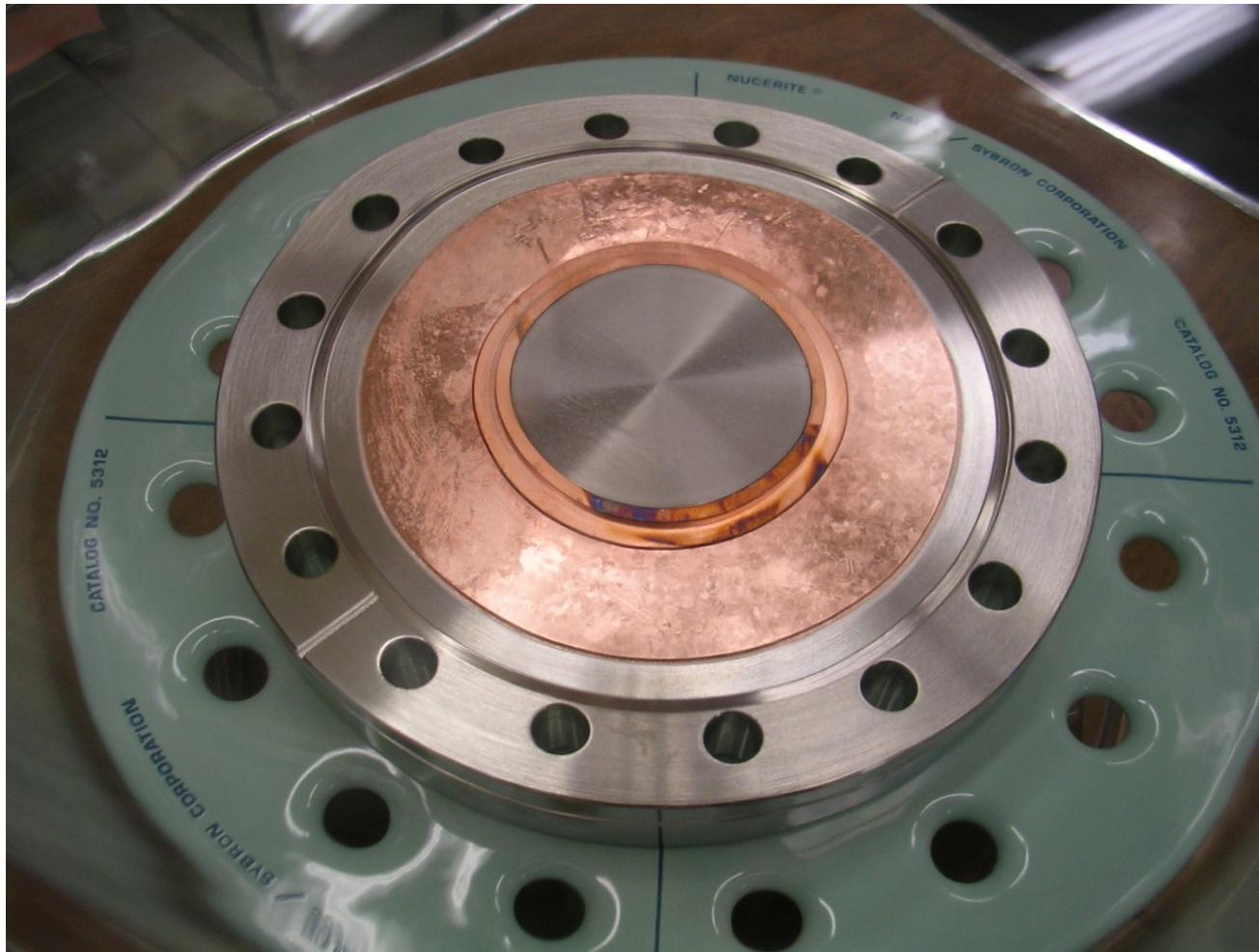
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## Photographs



# Overview: System Description

## Photographs



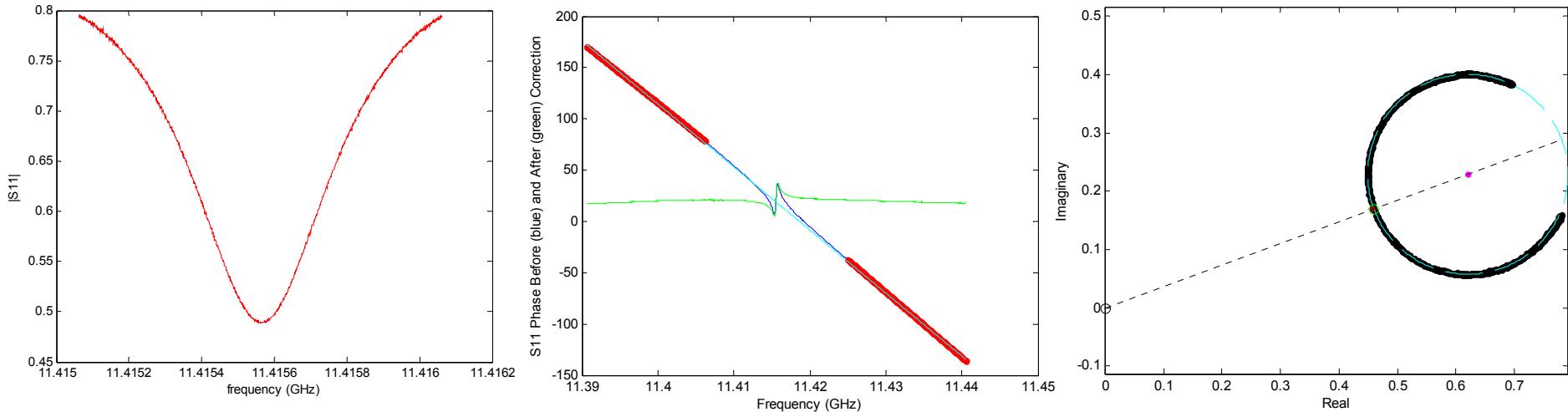
# Overview: System Description

## Photographs



# Overview: System Description

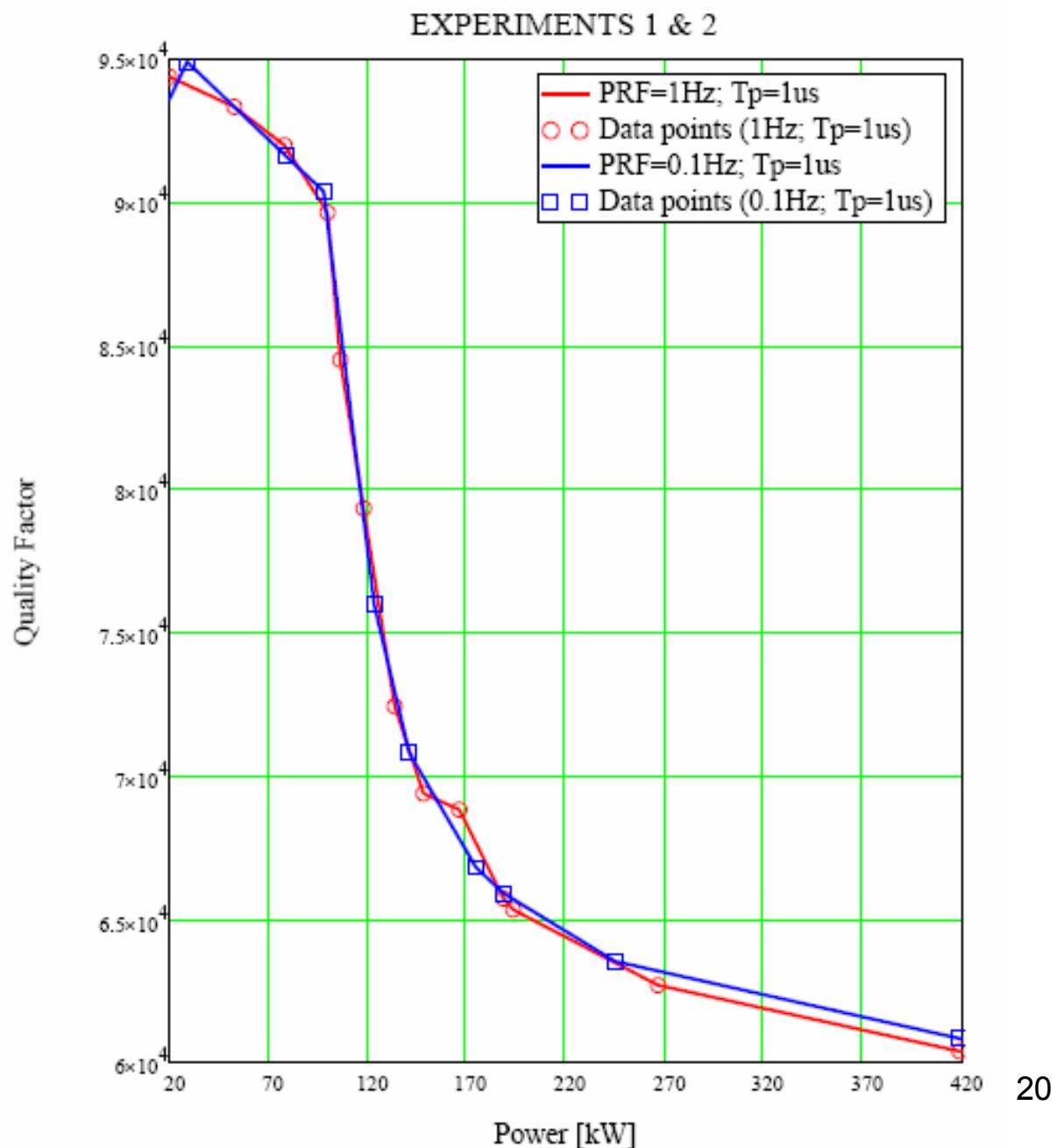
- Data Processing (room temperature)



- Complex  $S_{11}$  is measured with 1601 points in 1MHz around resonance.
- Phase slew due to input waveguide, determined from a 50 MHz measurement is subtracted from 1 MHz data.
- A “Q circle” is fit to the corrected  $S_{11}$  data in the complex plane to determine  $f_r$ ,  $\mathbf{b}$ , and  $\mathbf{Q}_L$ . From these  $\mathbf{Q}_0$  and  $\mathbf{Q}_e$  are derived.
- Temperature measured with a carbon-glass resistor (low end) inserted into a hole in bottom of cavity and from frequency shift (higher temperatures).

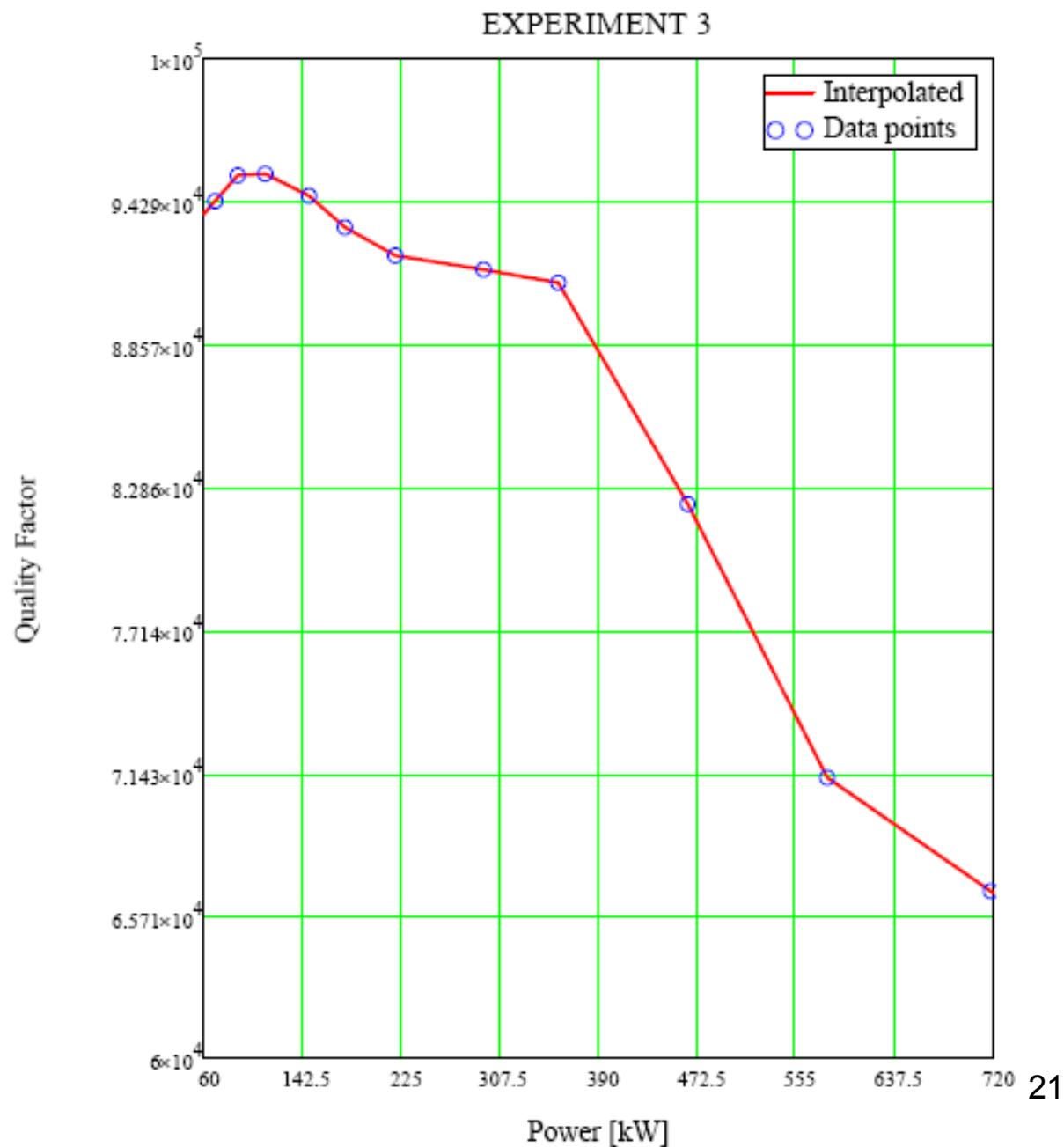
# Overview: Results

Nb: RRR = 250



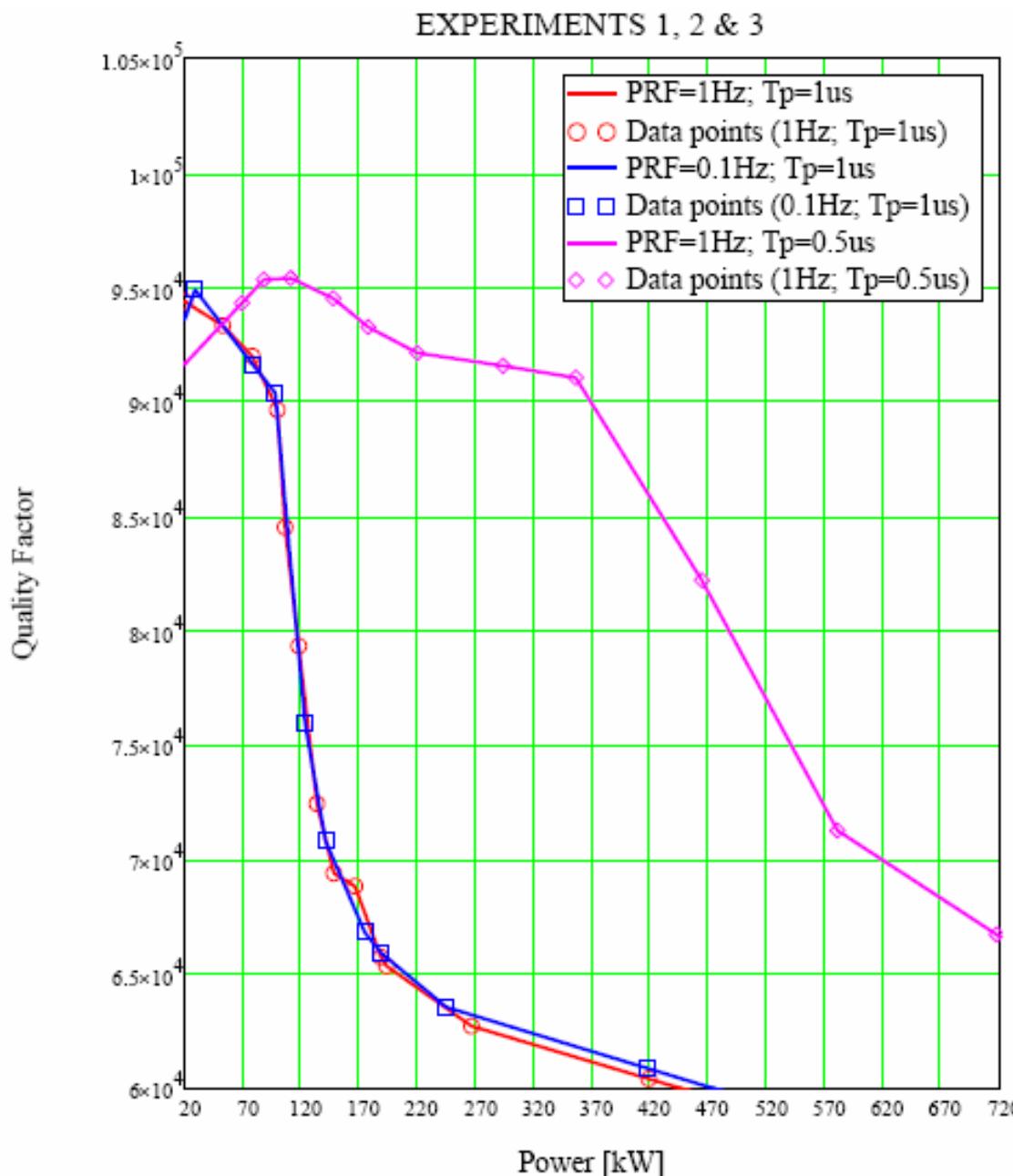
# Overview: Results

Nb: RRR = 250



# Overview: Results

Nb: RRR = 250



# Overview: Results

- How does the pulse width depends upon input power at a given  $Q_L$ ?
- How do we translate the incident power to critical magnetic field?
- How does the sample quench?

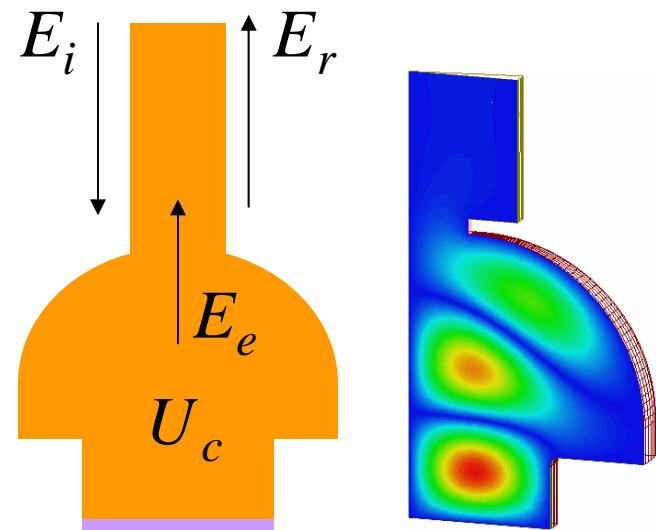
# Cavity Model: Pulse Dependence

- Power balance equation

$$-\frac{dU_c}{dt} + P_i - P_r - P_L = 0$$

$$E_r = E_e + \Gamma E_i$$

$$-\frac{dU_c}{dt} + E_i^2 - (E_e + \Gamma E_i)^2 - P_L = 0$$



$$U_c = \alpha E_e^2$$

$$P_L = \xi U_c$$

# Cavity Model: Pulse Dependence

- Power balance equation

$$-\frac{dU_c}{dt} + E_i^2 - \left( E_e^2 + \Gamma^2 E_i^2 + 2E_e \Gamma E_i \right) - \xi U_c = 0$$

$$-\frac{dU_c}{dt} + E_i^2 \left( 1 - \Gamma^2 \right) - E_e^2 - 2E_e \Gamma E_i - \xi U_c = 0$$

$$\Gamma \approx -1 \quad \frac{dU_c}{dt} + E_e^2 + \xi U_c = 2E_e E_i$$

$$\frac{d\alpha E_e^2}{dt} + E_e^2 + \xi \alpha E_e^2 = 2E_e E_i$$

# Cavity Model: Pulse Dependence

- Power balance equation

$$2\alpha \cancel{E_e} \frac{dE_e}{dt} + E_e^2 + \xi \alpha E_e^2 = 2 \cancel{E_e} E_i$$

$$\frac{dE_e}{dt} + \left( \frac{1 + \xi \alpha}{2\alpha} \right) E_e = \frac{E_i}{\alpha}$$

Recall

$$U_c = \alpha E_e^2 \quad \beta = \frac{P_e}{P_L} \Rightarrow Q_0 = \frac{\omega_0 \beta U_c}{E_e^2} \Rightarrow U_c = \frac{Q_0}{\omega_0 \beta} E_e^2 \Rightarrow \alpha = \frac{Q_0}{\omega_0 \beta}$$

$$P_L = \xi U_c \quad Q_0 = \frac{\omega_0 U_c}{P_L} \Rightarrow P_L = \frac{\omega_0}{Q_0} U_c \Rightarrow \xi = \frac{\omega_0}{Q_0}$$

# Cavity Model: Pulse Dependence

- Power balance equation

$$\frac{1+\xi\alpha}{2\alpha} = \frac{\omega_0}{2Q_0}(1+\beta)$$

$$\frac{1}{\alpha} = \frac{\omega_0\beta}{Q_0}$$



$$\frac{dE_e}{dt} + \frac{\omega_0}{2Q_0}(1+\beta)E_e = \frac{\omega_0\beta}{Q_0}E_i$$

Given  $Q_L = \frac{Q_0}{1+\beta}$



$$\frac{2Q_L}{\omega_0} \frac{dE_e}{dt} = \frac{2\beta}{1+\beta} E_i - E_e$$

Also

$$\beta = \frac{Q_0}{Q_e}, Q_L = \frac{Q_0}{1+\beta}$$



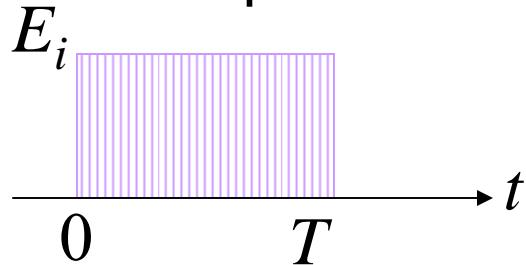
$$\frac{2\beta}{1+\beta} = \frac{2Q_L}{Q_e}$$

# Cavity Model: Pulse Dependence

- Power balance equation

General solution:  $E_e = \frac{2Q_L}{Q_e} E_i \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right)$

Incident pulse



$$E_i = \begin{cases} \sqrt{P_i} & 0 \leq t \leq T \\ 0 & t > T \end{cases}$$

$$E_e = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right) \quad 0 \leq t \leq T$$
$$E_e = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T}{2Q_L}} \right) e^{-\frac{\omega_0(t-T)}{2Q_L}} \quad t > T$$

# Cavity Model: Pulse Dependence

- Reflected field

Recall

$$E_r = E_e + \Gamma E_i \Rightarrow E_r = E_e - E_i$$

$$E_r = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right) - \sqrt{P_i} \quad 0 \leq t \leq T$$
$$E_r = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T}{2Q_L}} \right) e^{-\frac{\omega_0(t-T)}{2Q_L}} \quad t > T$$

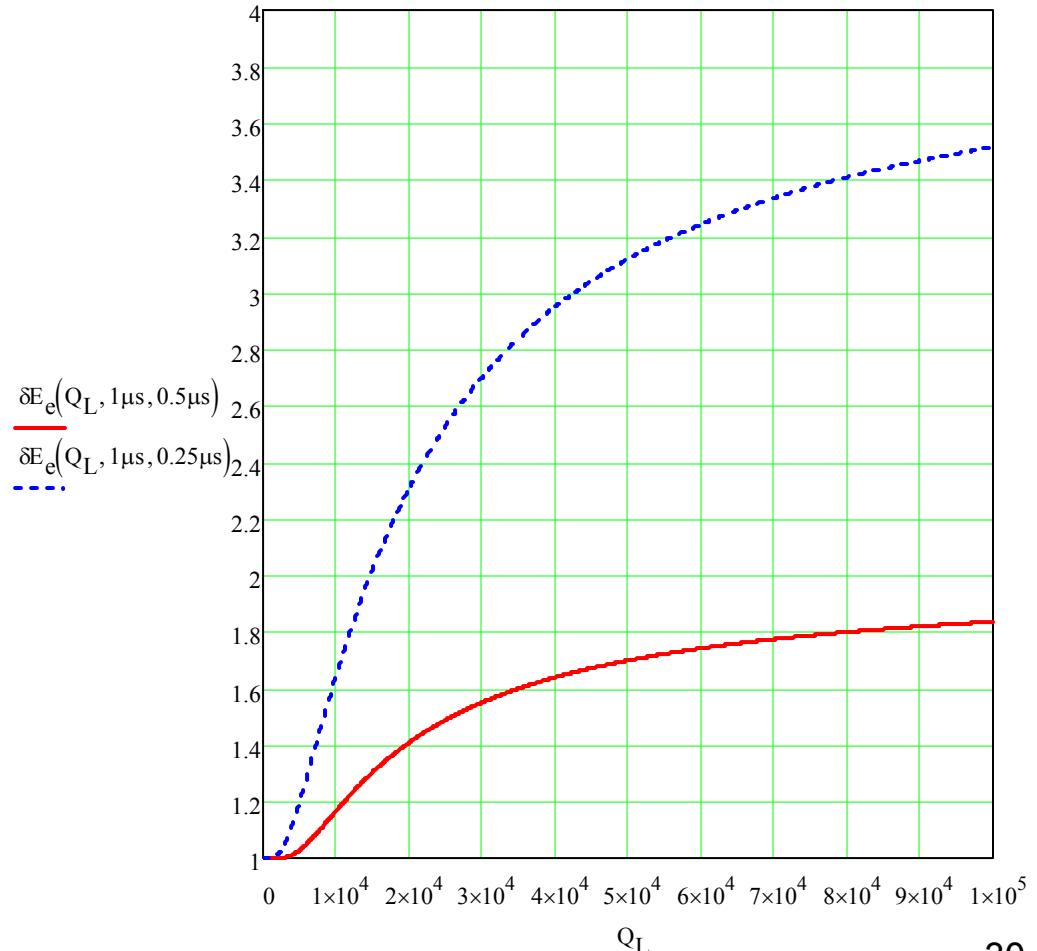
# Cavity Model: Pulse Dependence

- Maximum exiting field

$$E_e^{\max}(T = T_1) = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right)$$

$$E_e^{\max}(T = T_2) = \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T_2}{2Q_L}} \right)$$

$$\delta E_e(Q_L, T_1, T_2) = \frac{\left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right)}{\left( 1 - e^{-\frac{\omega_0 T_2}{2Q_L}} \right)}$$



# Cavity Model: Pulse Dependence

- Reflected power

$$P_r = E_r^2 = \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right) - \sqrt{P_i} \right]^2 \quad 0 \leq t \leq T$$

$$P_r = E_r^2 = \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T}{2Q_L}} \right) e^{-\frac{\omega_0(t-T)}{2Q_L}} \right]^2 \quad t > T$$

# Cavity Model: Pulse Dependence

- Reflected power

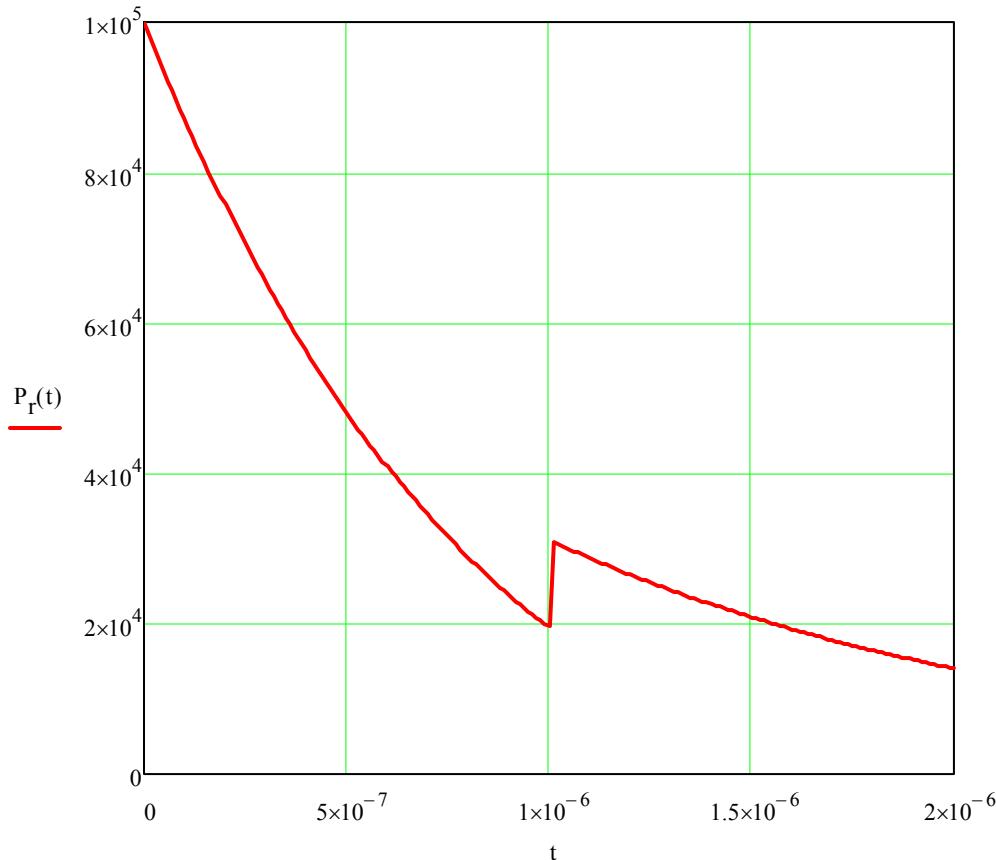
$$Q_e = 106000$$

$$Q_L = 90000$$

$$f_0 = 11.4\text{GHz}$$

$$P_i = 100\text{kW}$$

$$T = 1\mu\text{s}$$



# Cavity Model: Pulse Dependence

- Power in the cavity

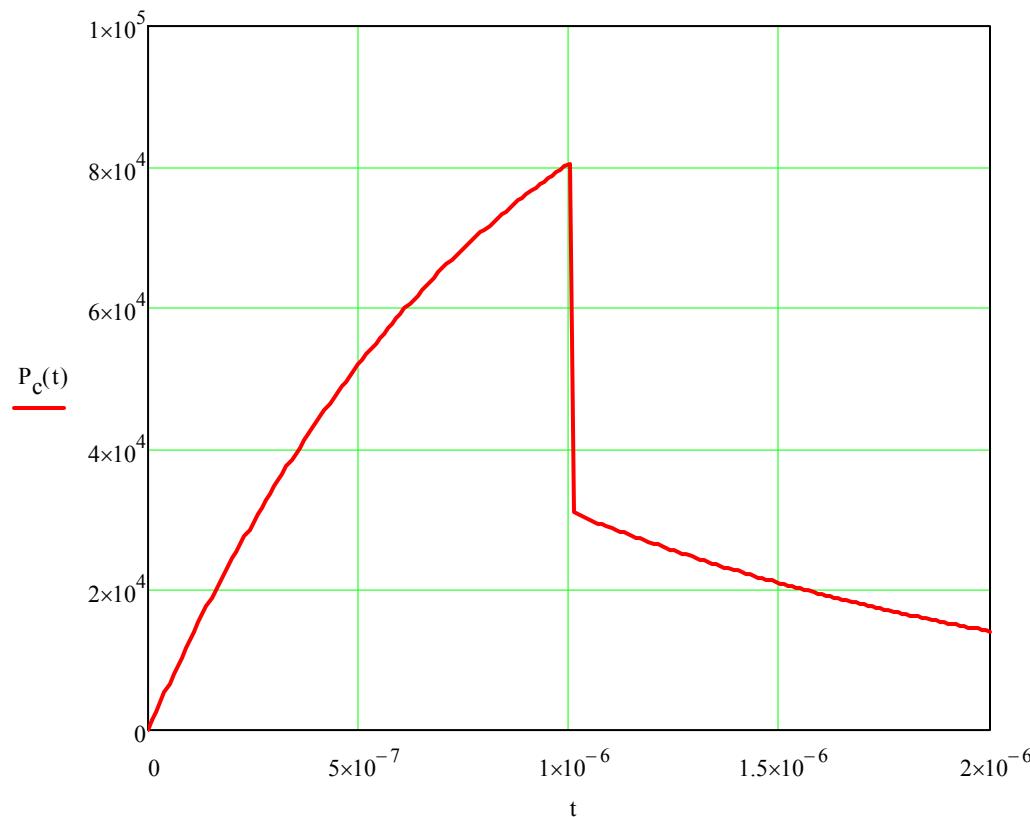
$$P_c = P_i - P_r$$

$$P_c = P_i - \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right) - \sqrt{P_i} \right]^2 \quad 0 \leq t \leq T$$

$$P_c = \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T}{2Q_L}} \right) e^{-\frac{\omega_0(t-T)}{2Q_L}} \right]^2 \quad t > T$$

# Cavity Model: Pulse Dependence

- Power in the cavity



$$Q_e = 106000$$

$$Q_L = 90000$$

$$f_0 = 11.4\text{GHz}$$

$$P_i = 100\text{kW}$$

$$T = 1\mu\text{s}$$

# Cavity Model: Pulse Dependence

- Maximum power in the cavity

$$P_c^{\max}(T = T_1) = P_i - \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right) - \sqrt{P_i} \right]^2$$
$$P_c^{\max}(T = T_2) = P_i - \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T_2}{2Q_L}} \right) - \sqrt{P_i} \right]^2$$

$$\delta P_c(Q_L, T_1, T_2) = \frac{P_c^{\max}(T = T_1)}{P_c^{\max}(T = T_2)}$$

# Cavity Model: Pulse Dependence

- Maximum power in the cavity

$$\begin{aligned} P_c^{\max}(T = T_1) &= P_i - \left[ \frac{2Q_L}{Q_e} \sqrt{P_i} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right) - \sqrt{P_i} \right]^2 \Rightarrow \\ &\Rightarrow P_i - \left[ \frac{4Q_L^2}{Q_e^2} P_i \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right)^2 + P_i - P_i \frac{4Q_L}{Q_e} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right) \right] \Rightarrow \\ &4P_i \frac{Q_L}{Q_e} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right) \cdot \left[ 1 - \frac{Q_L}{Q_e} \left( 1 - e^{-\frac{\omega_0 T_1}{2Q_L}} \right) \right] \end{aligned}$$

# Cavity Model: Pulse Dependence

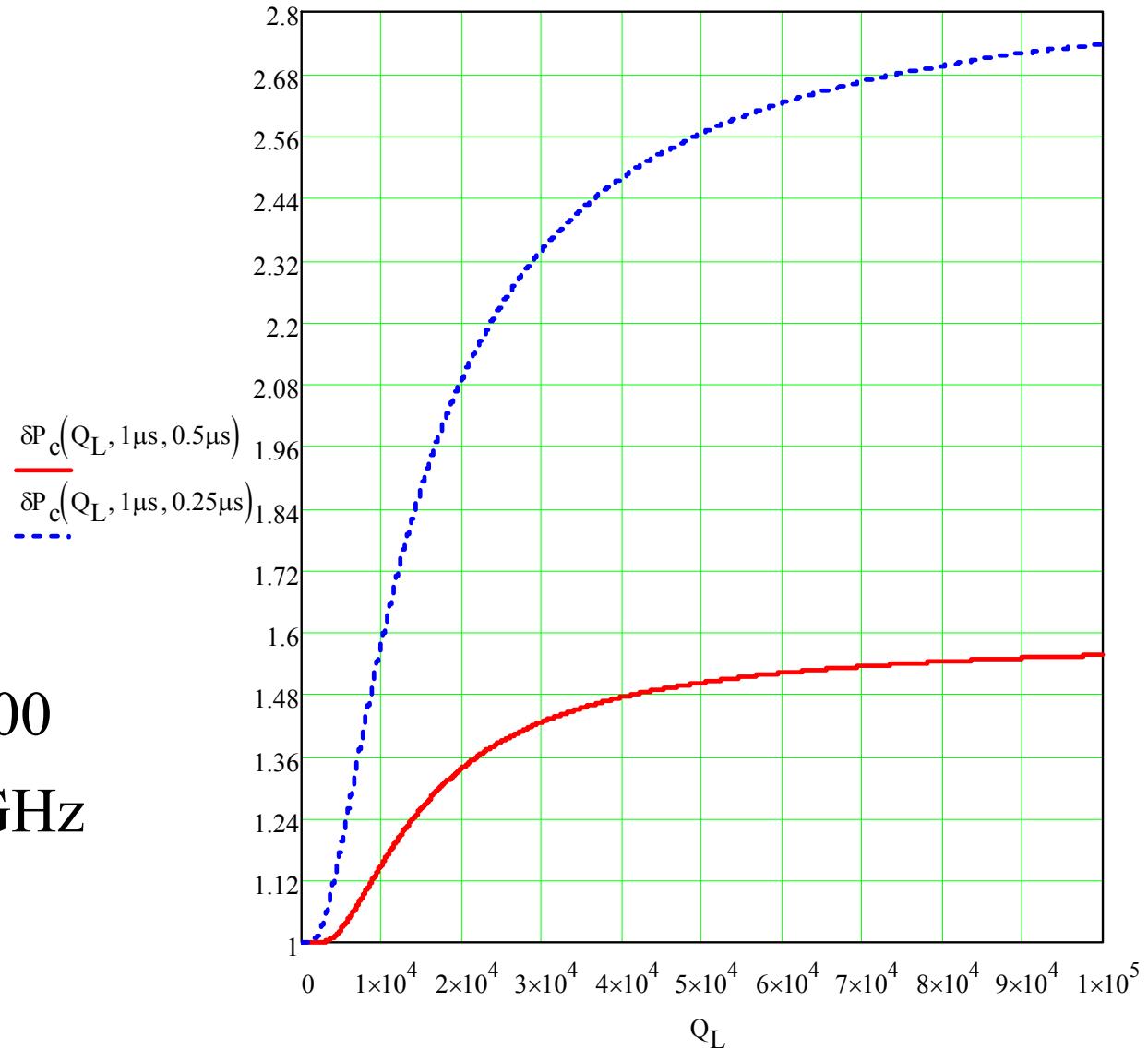
- Ratio of maximum power in the cavity for different pulse lengths

$$\delta P_c(Q_L, T_1, T_2) = \frac{\left(1 - e^{-\frac{\omega_0 T_1}{2Q_L}}\right) \cdot \left[1 - \frac{Q_L}{Q_e} \left(1 - e^{-\frac{\omega_0 T_1}{2Q_L}}\right)\right]}{\left(1 - e^{-\frac{\omega_0 T_2}{2Q_L}}\right) \cdot \left[1 - \frac{Q_L}{Q_e} \left(1 - e^{-\frac{\omega_0 T_2}{2Q_L}}\right)\right]}$$

# Cavity Model: Pulse Dependence

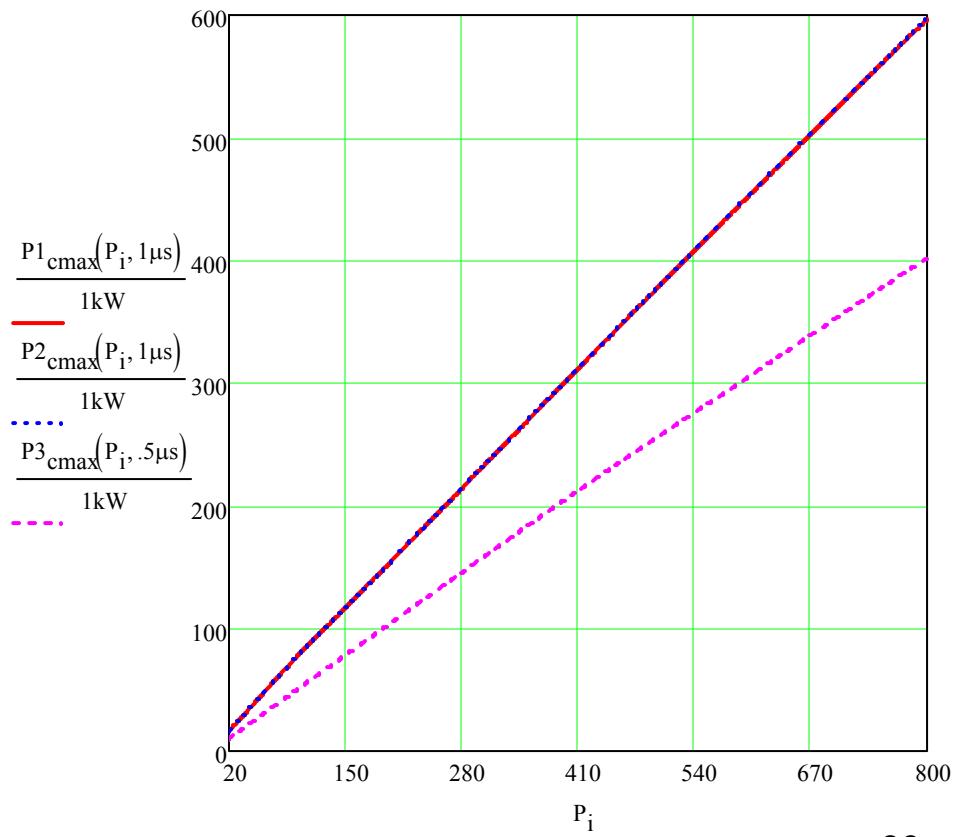
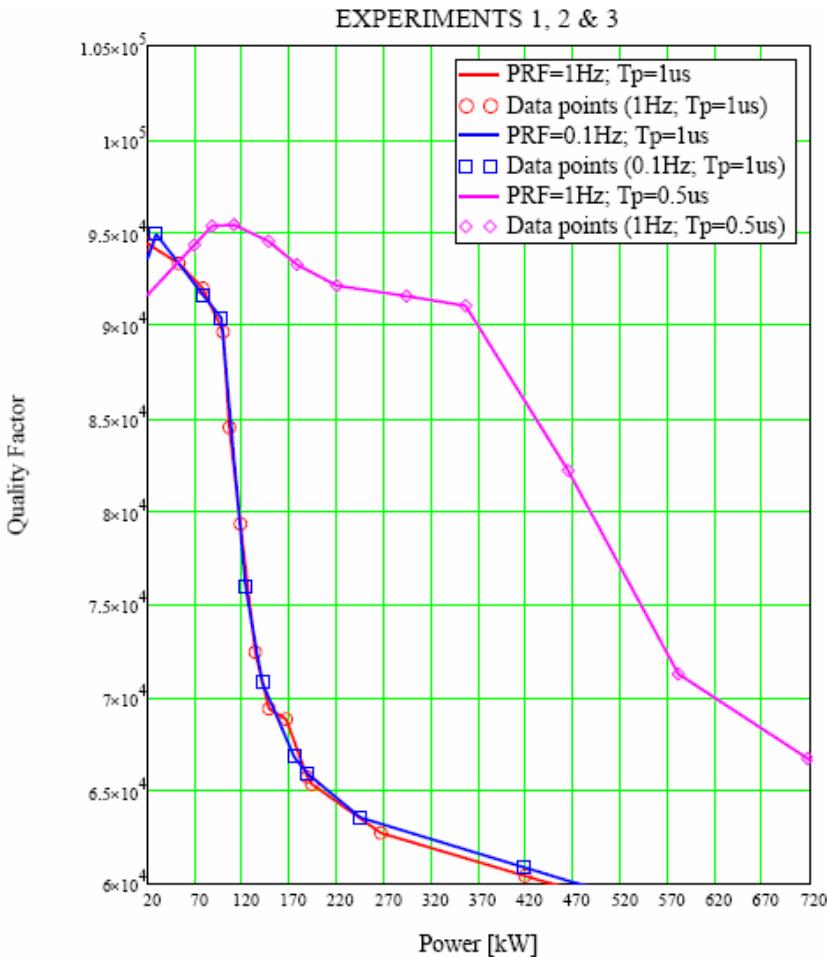
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$$f_0 = 11.4\text{GHz}$$



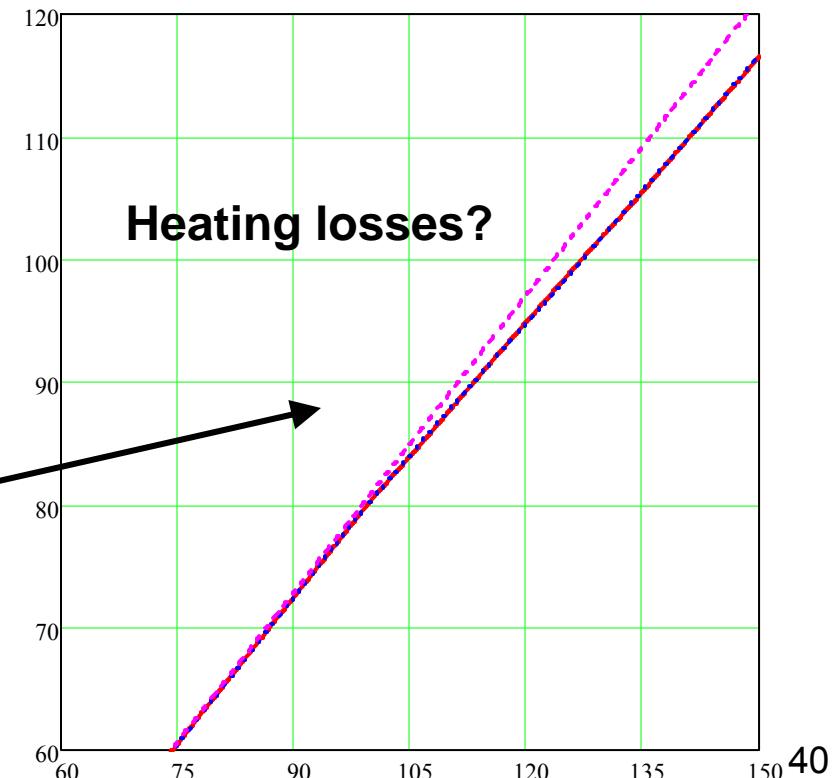
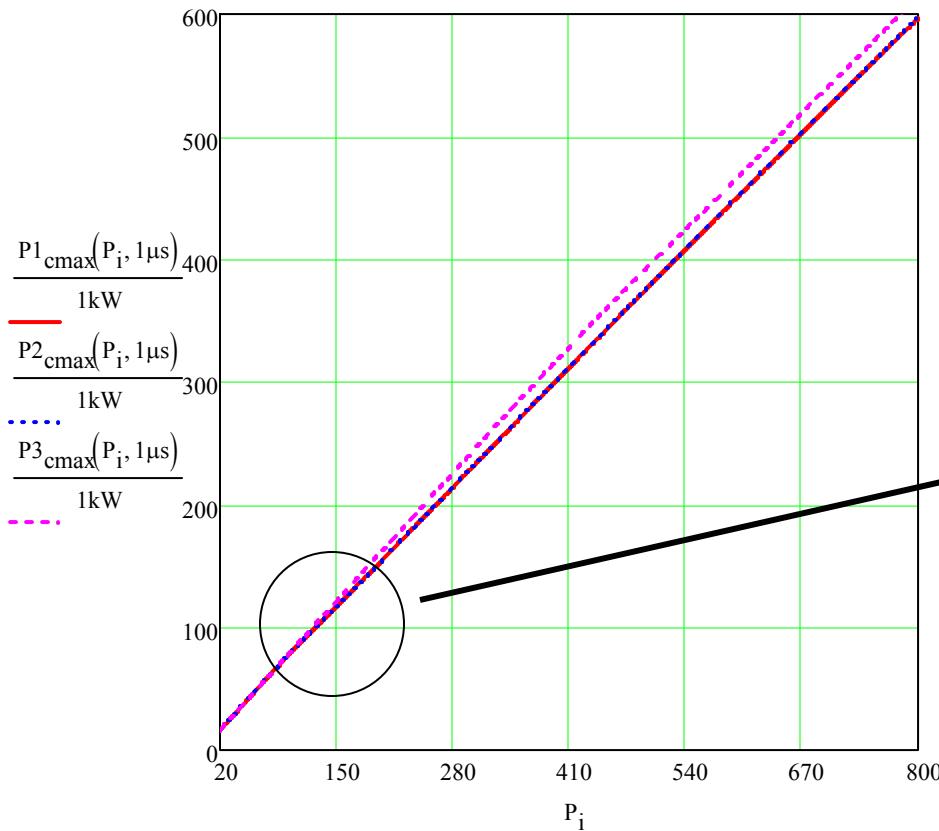
# Cavity Model: Pulse Dependence

- Maximum power in the cavity for the three experiments versus  $P_i$



# Cavity Model: Pulse Dependence

- Maximum power in the cavity for the three experiments versus  $P_i$ 
  - If experiment 3 were 1μs,  $P_c$  should be similar to those in experiments 1 & 2.

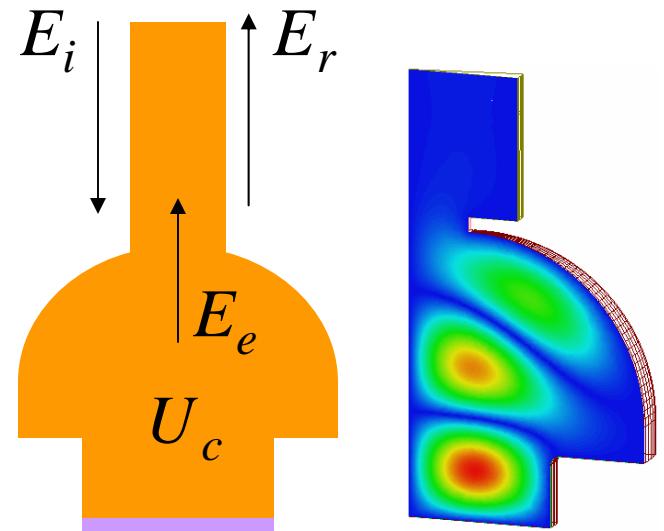


# Cavity Model: Critical Magnetic Field

- Quality factors

$$\frac{1}{Q_L} = \frac{1}{Q_e} + \frac{1}{Q_c} + \frac{1}{Q_s}$$

External (aperture)      Copper      Sample



- Fully superconducting sample

$$Q_s = \infty \Rightarrow \frac{1}{Q_L} = \frac{1}{Q_e} + \frac{1}{Q_c} \Rightarrow \frac{1}{Q_c} = \frac{1}{Q_L} - \frac{1}{Q_e}$$

# Cavity Model: Critical Magnetic Field

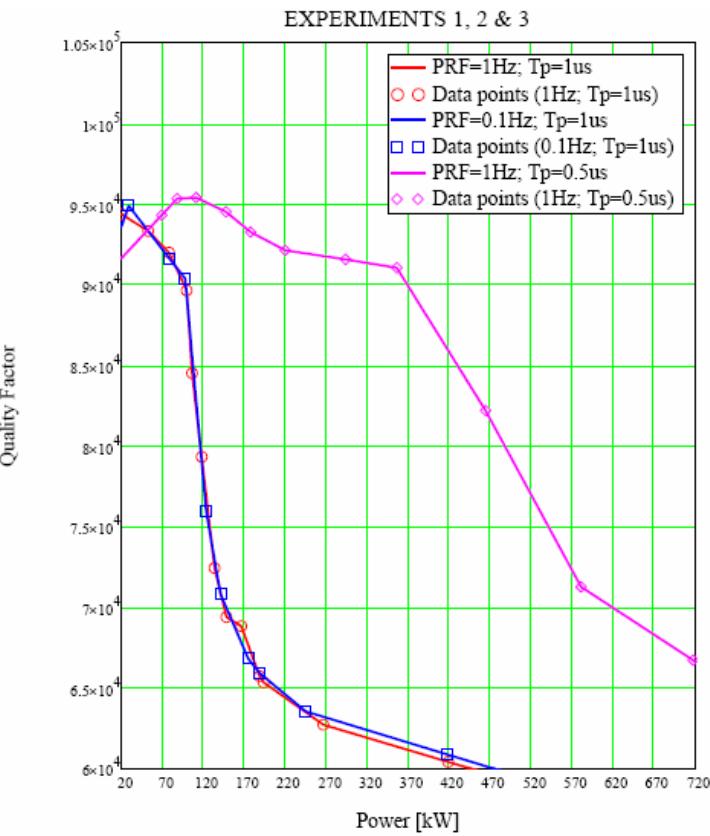
- Quality factor in normal conducting state
  - Fully superconducting

$$Q_L \approx 95000 \Rightarrow Q_c = 915455$$

- Fully normal conducting

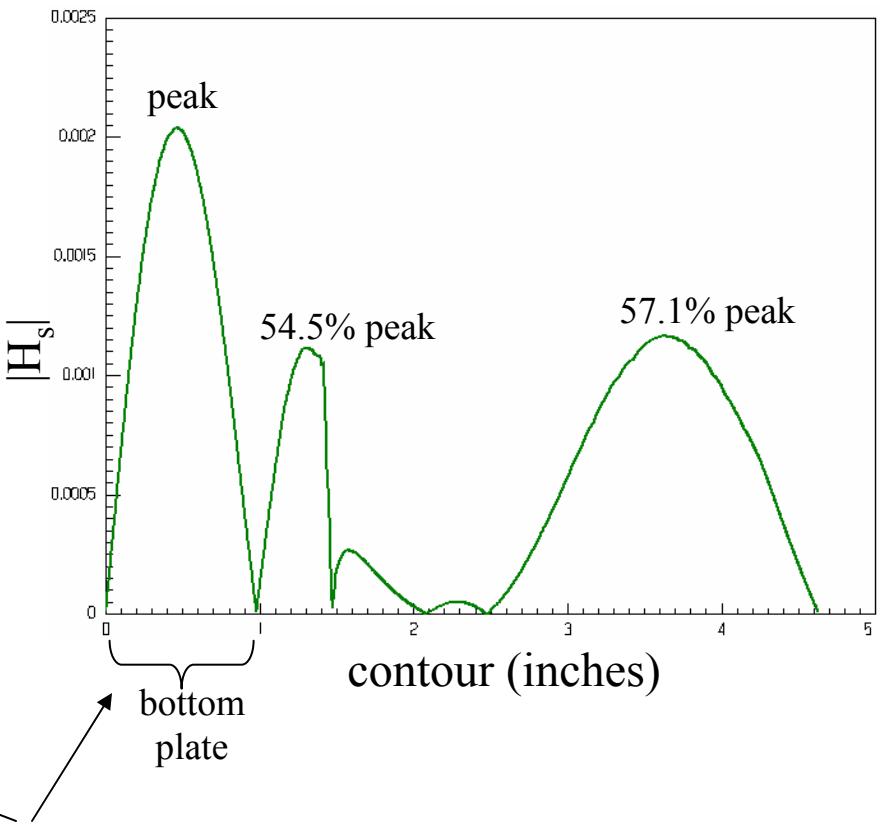
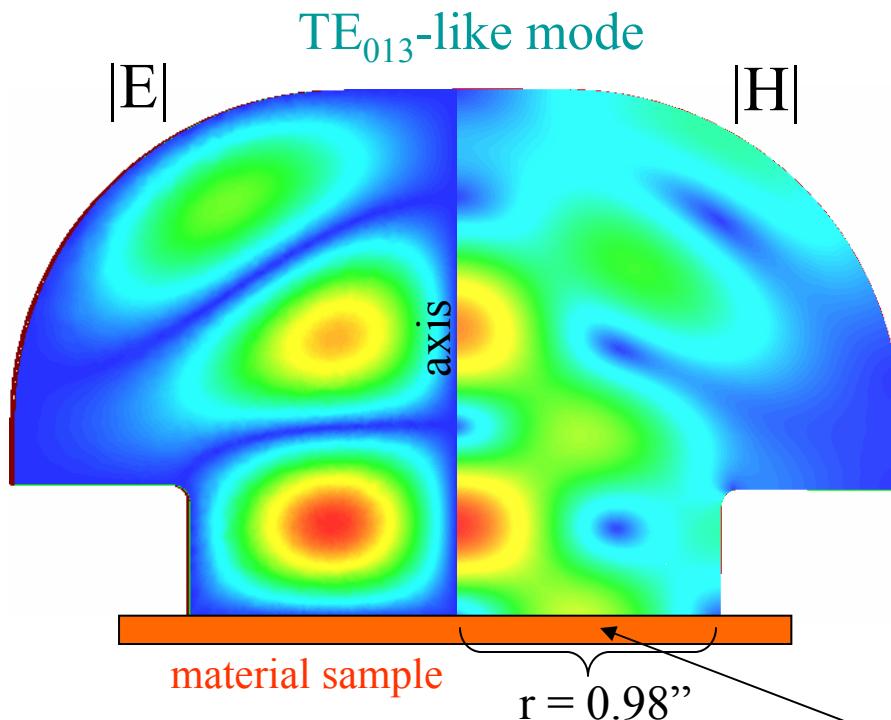
$$\frac{1}{Q_s} = \frac{1}{Q_L} - \frac{1}{Q_e} - \frac{1}{Q_c}$$

$$Q_L \approx 60000 \Rightarrow Q_s^{nc} = 162857$$



# Cavity Model: Critical Magnetic Field

- Surface magnetic field



**Bessel function of 1<sup>st</sup> order  
of the 1<sup>st</sup> kind,  $J_1(x)$**

# Cavity Model: Critical Magnetic Field

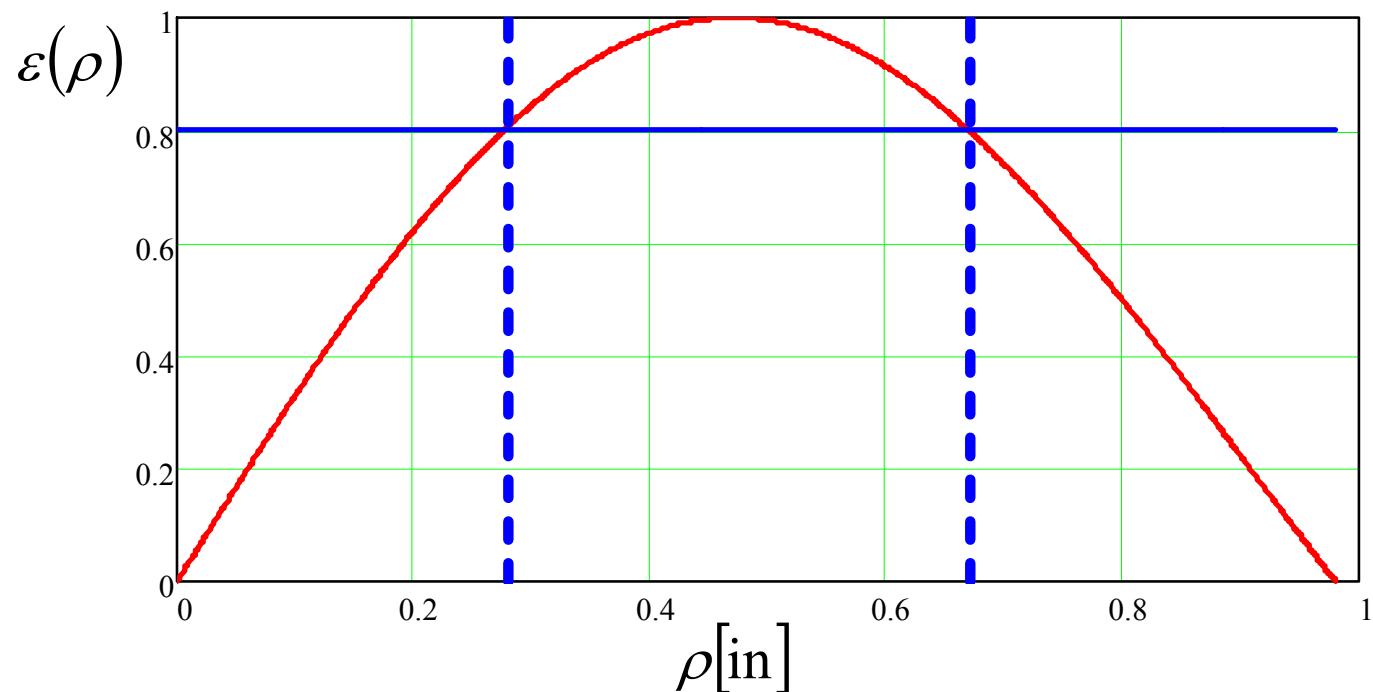
- Surface magnetic field

radius  $a = 0.98''$

$$H_s(\rho) \propto J_1\left(\frac{3.8317\rho}{a}\right)$$

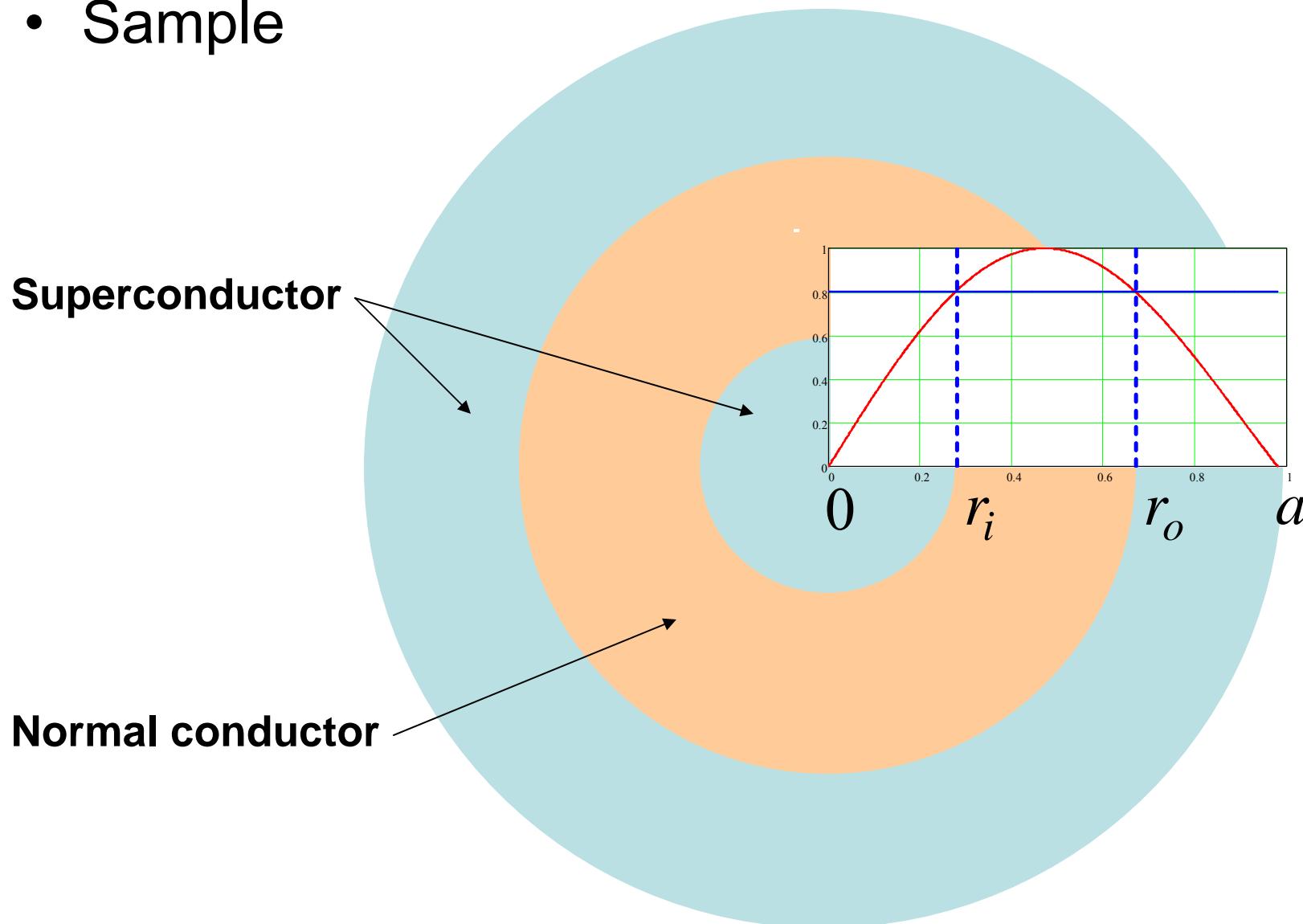
$$\varepsilon(\rho) = \frac{H_s(\rho)}{\max[H_s(\rho)]}$$

**Normalized field**



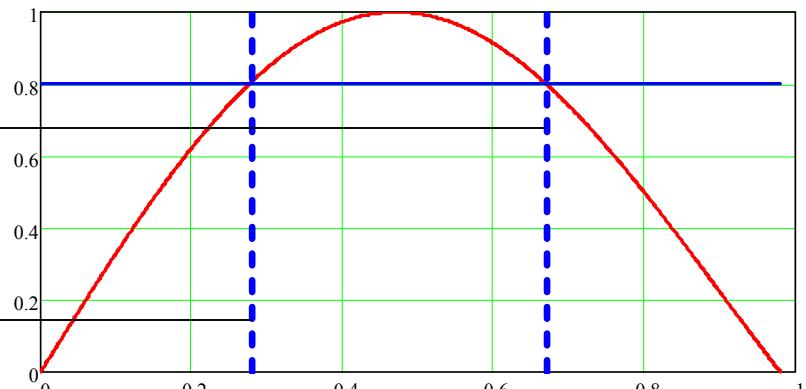
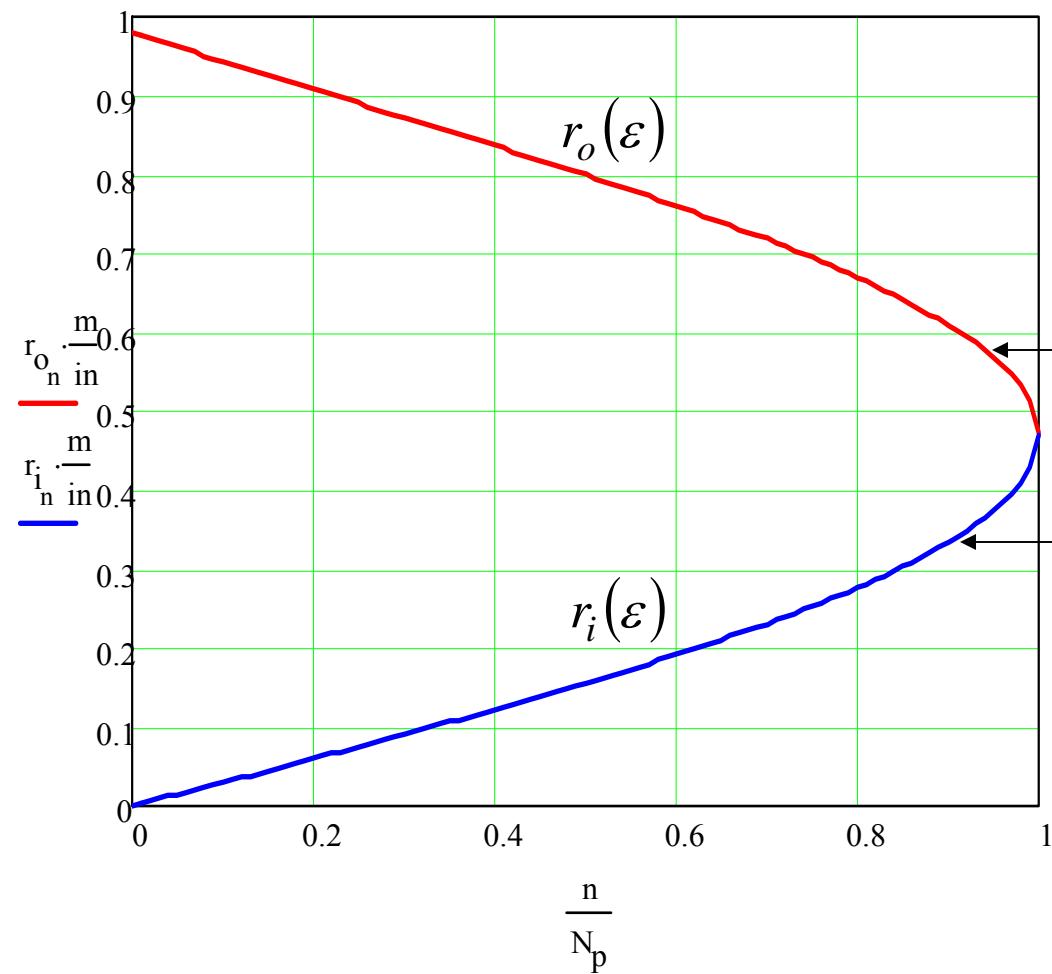
# Cavity Model: Critical Magnetic Field

- Sample



# Cavity Model: Critical Magnetic Field

- Inverse Bessel function

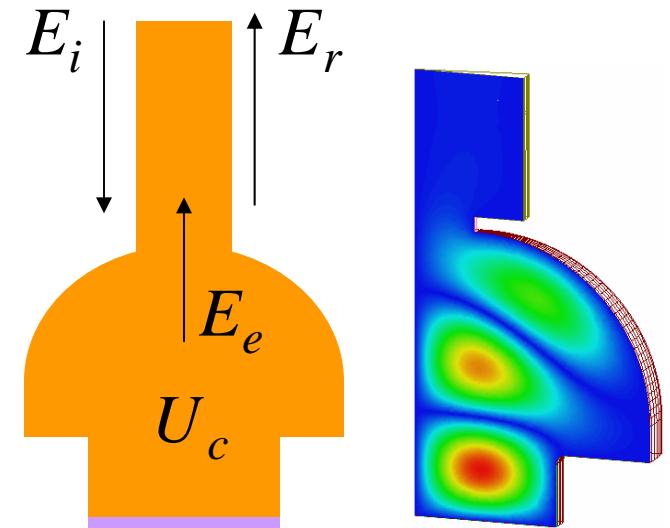


# Cavity Model: Critical Magnetic Field

- Quality factors

$$\frac{1}{Q_L} = \frac{1}{Q_e} + \frac{1}{Q_c} + \frac{1}{Q_s}$$

External (aperture)      Copper      Sample



$$Q_s = \frac{\omega_0 U_c}{R_s P_L^s} = \frac{\omega_0 \mu_0 \iiint_V |\epsilon(\rho)|^2 dv}{R_s \iiint_S |\epsilon(\rho)|^2 ds}$$

$$Q_s = \frac{\omega_0 \mu_0 \iiint_V |\epsilon(\rho)|^2 dv}{R_s \int_{r_i}^{r_o} 2\pi\rho |\epsilon(\rho)|^2 d\rho}$$

# Cavity Model: Critical Magnetic Field

- Sample quality factor

$$Q_s = \frac{\omega_0 \mu_0 \iiint_v |\varepsilon(\rho)|^2 dv}{R_s \int_{r_i}^{r_o} 2\pi\rho |\varepsilon(\rho)|^2 d\rho} \cdot \frac{\int_0^{\rho=a} 2\pi\rho |\varepsilon(\rho)|^2 d\rho}{\int_0^{\rho=a} 2\pi\rho |\varepsilon(\rho)|^2 d\rho}$$

$$Q_s = Q_s^{nc} \cdot \frac{\int_0^{\rho=a} 2\pi\rho |\varepsilon(\rho)|^2 d\rho}{\int_{r_i}^{r_o} 2\pi\rho |\varepsilon(\rho)|^2 d\rho} = Q_s^{nc} \cdot \frac{9.322 \cdot 10^{-4}}{\int_{r_i}^{r_o} 2\pi\rho |\varepsilon(\rho)|^2 d\rho}$$

# Cavity Model: Critical Magnetic Field

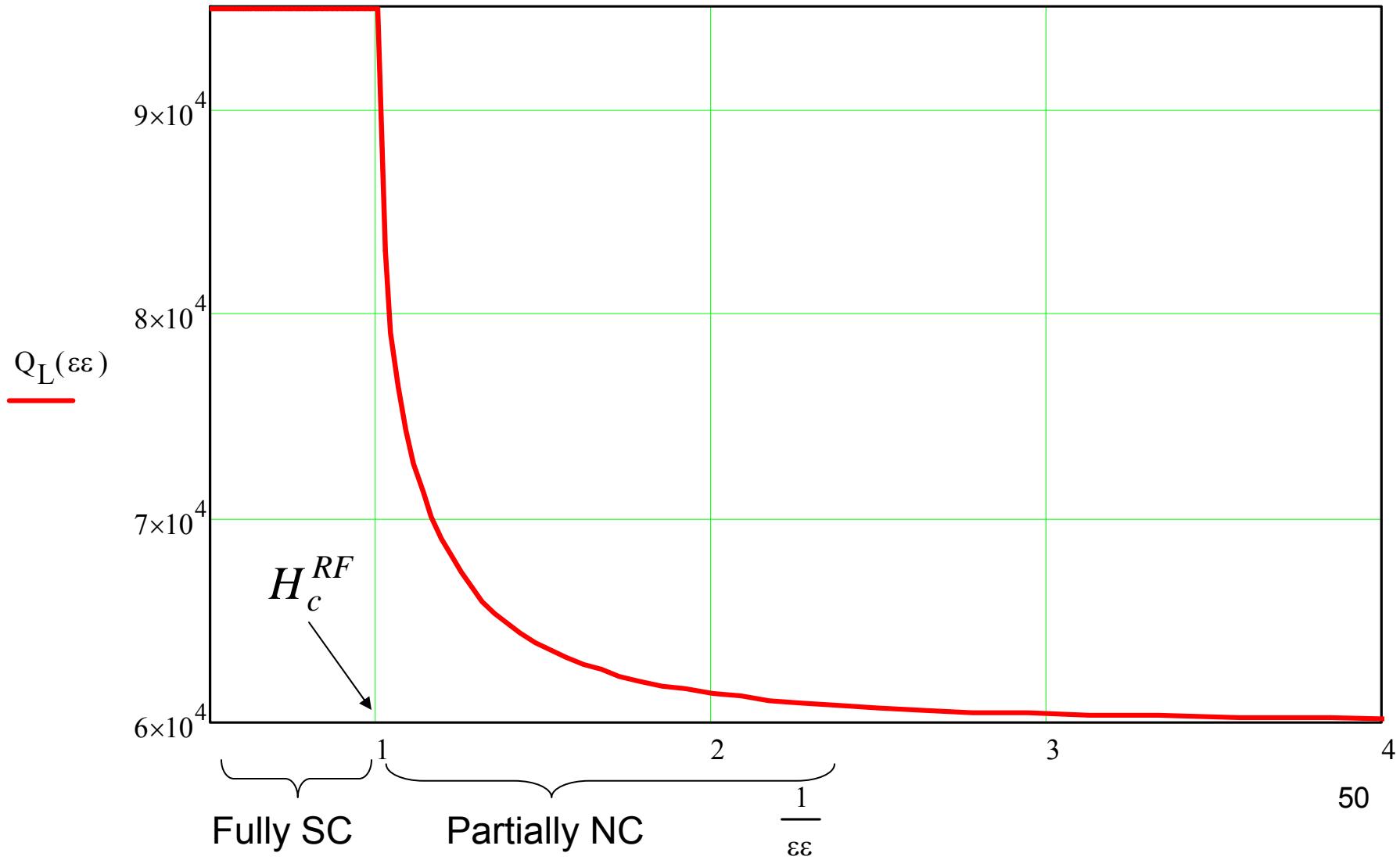
- Putting all together

$$\frac{1}{Q_L} = \frac{1}{Q_e} + \frac{1}{Q_c} + \frac{\int_{r_i}^{r_o} 2\pi\rho|\varepsilon(\rho)|^2 d\rho}{Q_s^{nc} \cdot 9.322 \cdot 10^{-4}}$$

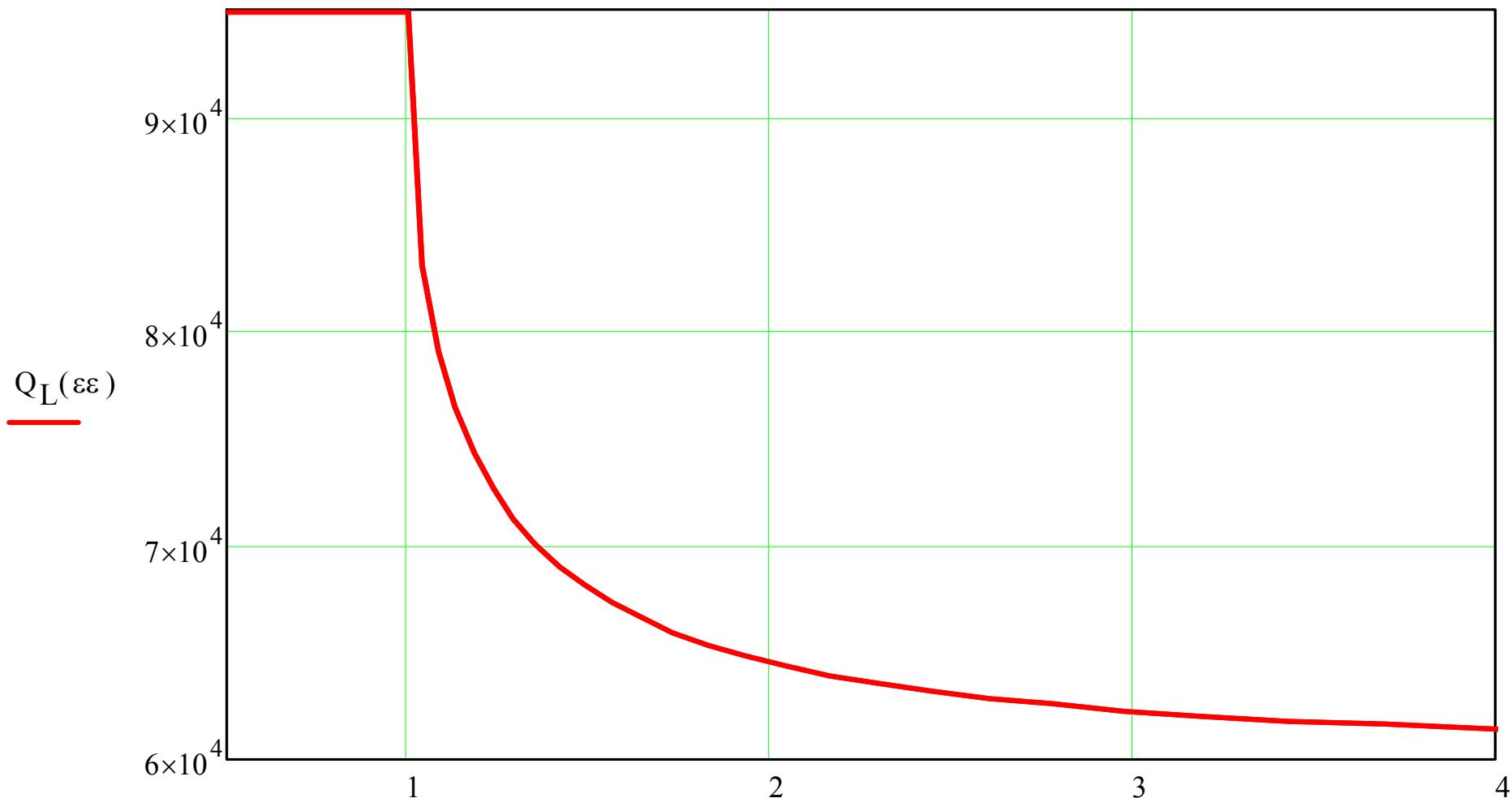
$$Q_L(\varepsilon) = \left[ \frac{1}{Q_e} + \frac{1}{Q_c} + \frac{\int_{r_i(\varepsilon)}^{r_o(\varepsilon)} 2\pi\rho|\varepsilon(\rho)|^2 d\rho}{Q_s^{nc} \cdot 9.322 \cdot 10^{-4}} \right]^{-1}$$

$$P \propto H_{\max}^2 \propto \left( \frac{H_c}{\varepsilon} \right)^2 \propto \left( \frac{1}{\varepsilon} \right)^2$$

# Cavity Model: Critical Magnetic Field



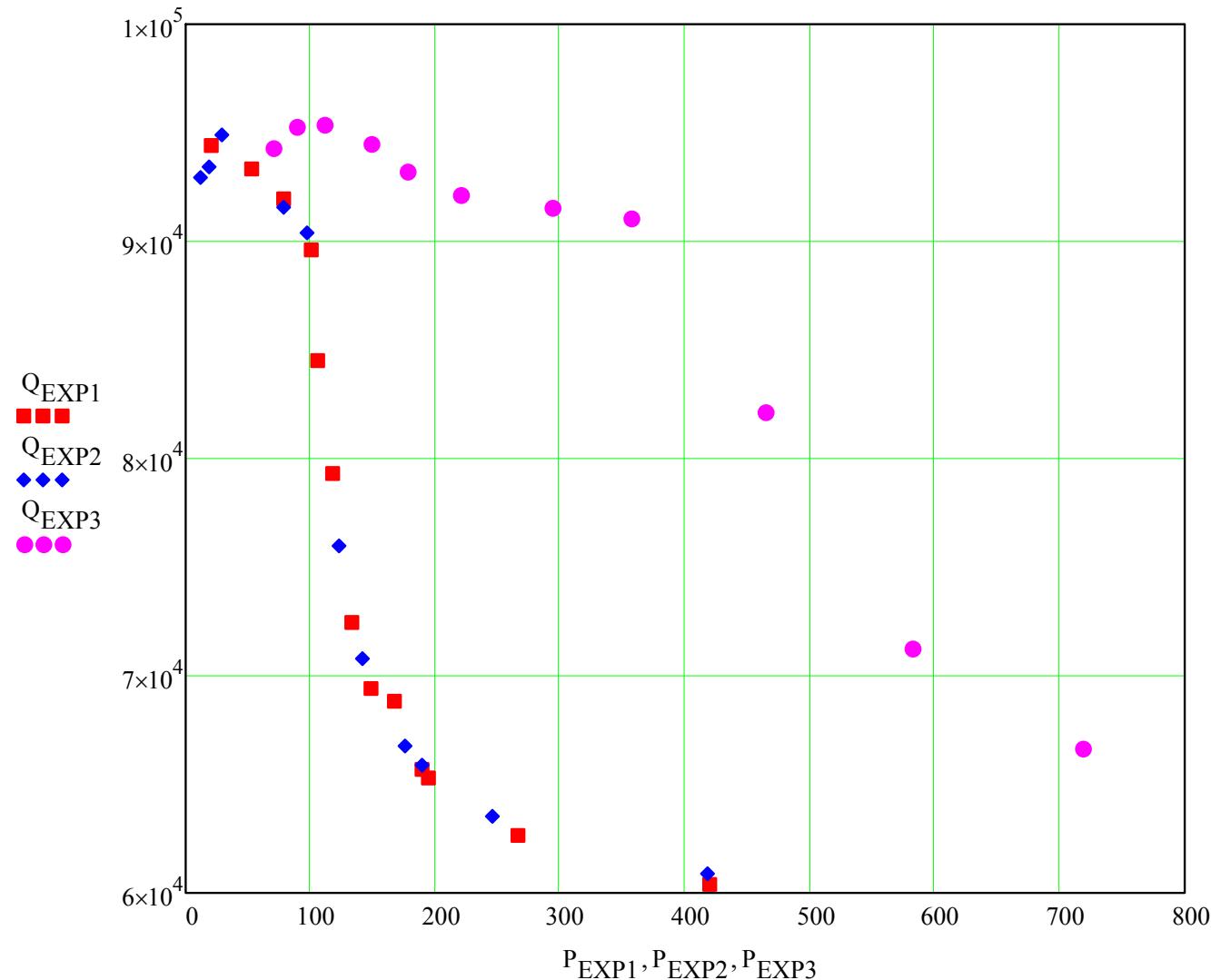
# Cavity Model: Critical Magnetic Field



$$\left(\frac{1}{\varepsilon\varepsilon}\right)^2$$

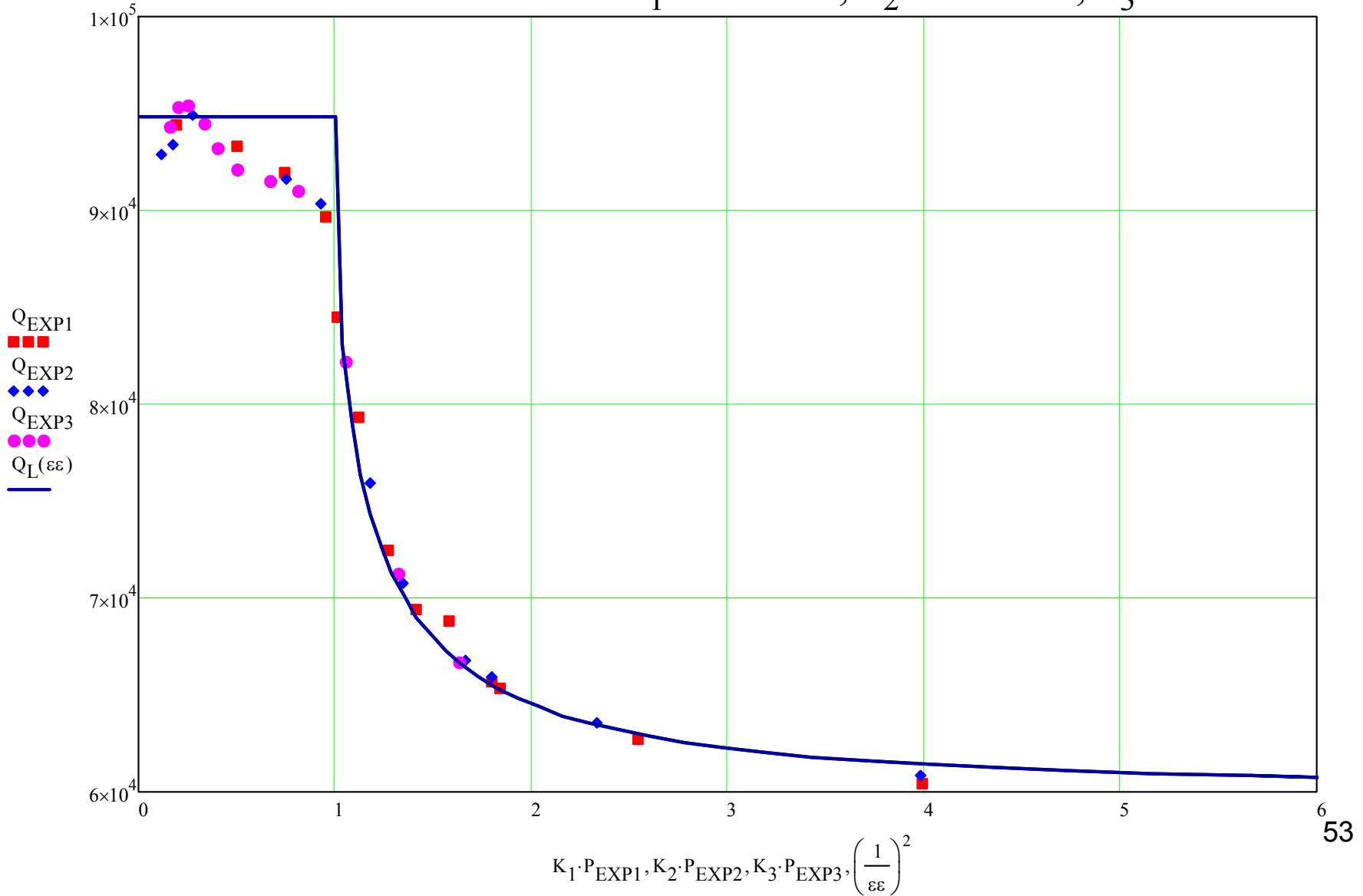
# Cavity Model: Critical Magnetic Field

- Experimental Data



# Cavity Model: Critical Magnetic Field

$$P_1 \rightarrow 1/105, P_2 \rightarrow 1/105, P_3 \rightarrow 1/440$$



# Cavity Model: Critical Magnetic Field

- Stored energy in steady state
  - From HFSS (Sami Tantawi)

$$U_c = 8.72265 \times 10^{-17} \text{ J} \Rightarrow |H_{\max}|^2 = 4.1048 \times 10^{-6} \frac{\text{A}^2}{\text{m}^2}$$

$$|H_{\max}|^2 = \zeta U_c \Rightarrow \zeta = 4.7059 \times 10^{10} \frac{\text{A}^2}{\text{m}^2 \text{J}}$$

- From MWS (Frank Krawczyk)

$$U_c = 1 \text{ J} \Rightarrow |H_{\max}|^2 = 4.614 \times 10^{10} \frac{\text{A}^2}{\text{m}^2}$$

$$|H_{\max}|^2 = \zeta U_c \Rightarrow \zeta = 4.614 \times 10^{10} \frac{\text{A}^2}{\text{m}^2 \text{J}}$$

Good agreement!

# Cavity Model: Critical Magnetic Field

- Maximum  $U_c$

$$U_c = \alpha E_e^2 = \frac{Q_o}{\omega_0 \beta} E_e^2 \Rightarrow U_c = \frac{Q_e}{\omega_0} E_e^2$$

$$U_c = \frac{4Q_L^2}{\omega_0 Q_e} P_i \left( 1 - e^{-\frac{\omega_0 t}{2Q_L}} \right)^2 \quad 0 \leq t \leq T$$

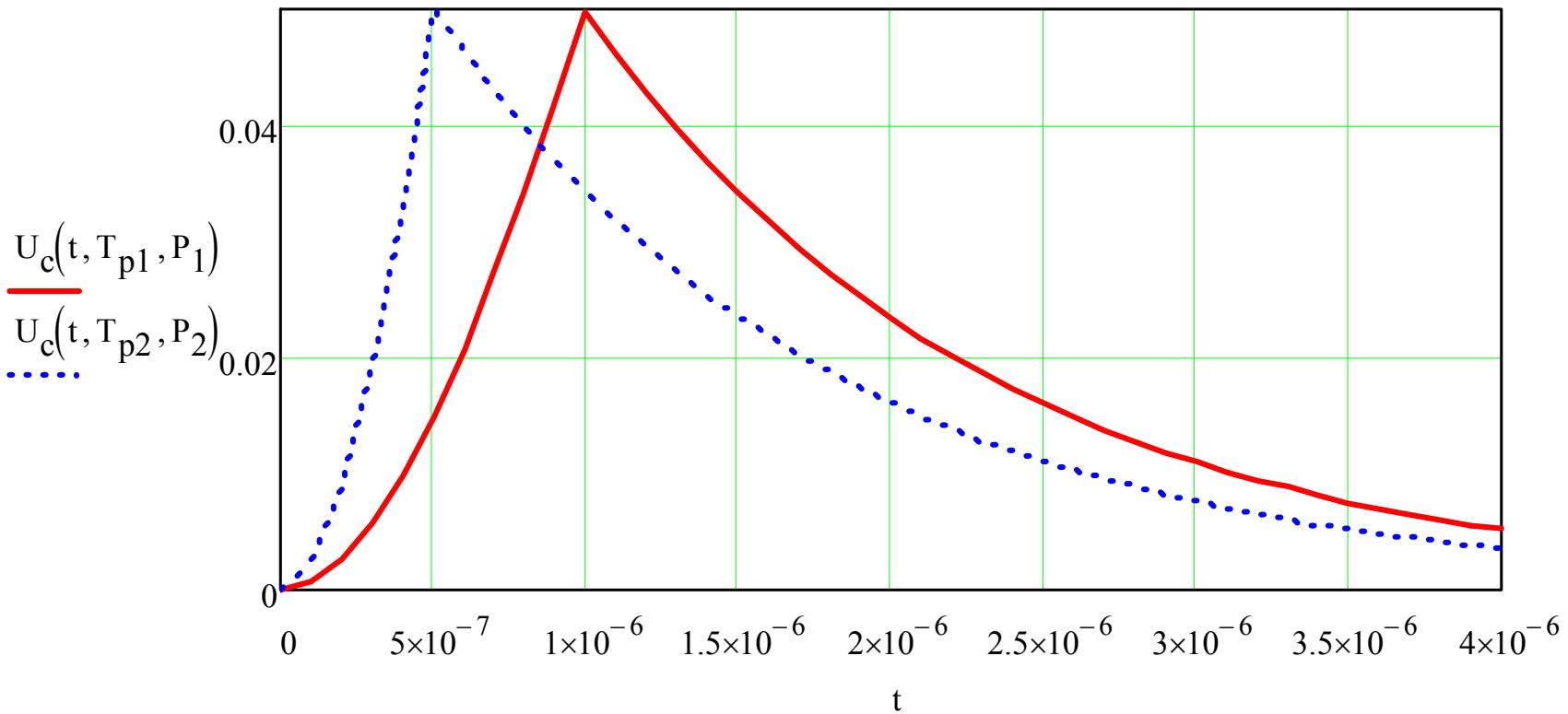
$$U_c = \frac{4Q_L^2}{\omega_0 Q_e} P_i \left( 1 - e^{-\frac{\omega_0 T}{2Q_L}} \right)^2 e^{-\frac{\omega_0(t-T)}{Q_L}} \quad t > T$$

# Cavity Model: Critical Magnetic Field

- Maximum  $U_c$

**1μs pulse:**  $T_{p1} := 1\mu s$   $P_1 := 106\text{kW}$

**.5μs pulse:**  $T_{p2} := .5\mu s$   $P_2 := 356\text{kW}$



# Cavity Model: Critical Magnetic Field

- Critical Magnetic Field

**1μs pulse:**

$$U_c(T_{p1}, T_{p1}, P_1) = 0.05J \quad H1_m := \sqrt{\zeta \cdot U_c(T_{p1}, T_{p1}, P_1)} \quad H1_m = 4.789 \times 10^4 \frac{A}{m}$$

$$B(H1_m) = 60.186 \text{ mT}$$

**.5μs pulse:**

$$U_c(T_{p2}, T_{p2}, P_2) = 0.05J \quad H2_m := \sqrt{\zeta \cdot U_c(T_{p2}, T_{p2}, P_2)} \quad H2_m = 4.801 \times 10^4 \frac{A}{m}$$

$$B(H2_m) = 60.331 \text{ mT}$$

# Results vs Model

## Discussion

- Nb should have a  $H_c^{RF}$  of at least ~180mT
- Possible causes
  - Pulsed heating not into account  
Solution: Use smaller and smaller pulses... available power is not an issue
  - Temperature in the RF surface is not 4.2K 60mT, assuming 180mT being the real critical field implies T=7.5K  
This could explain why other samples “never” became superconducting...

# Results vs Model

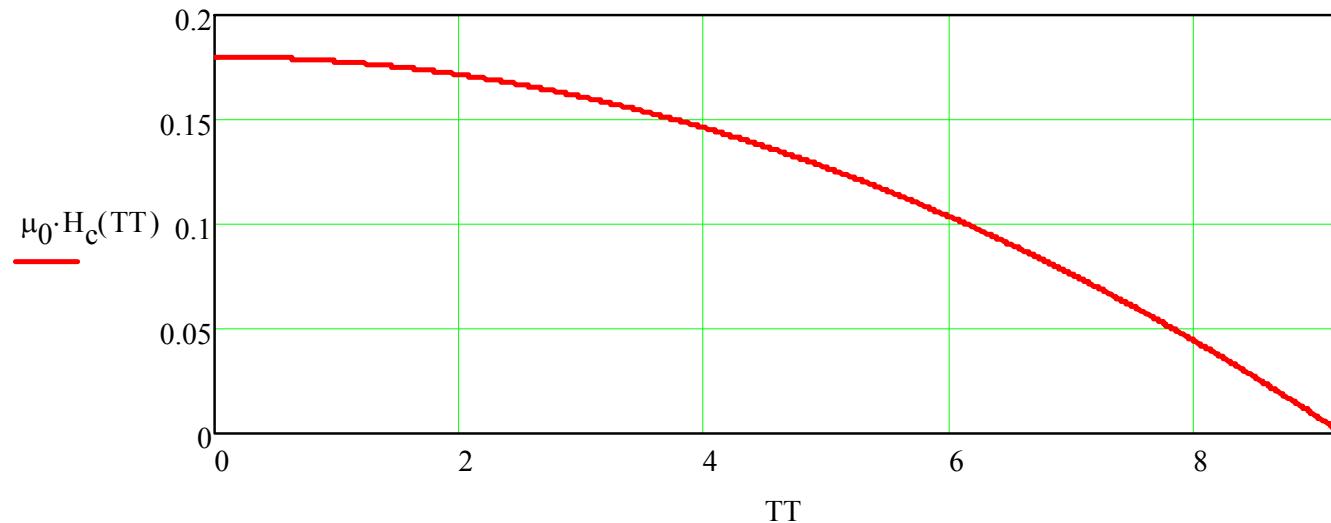
## Discussion

$$B_{cNb} := 180 \text{ mT} \quad H_{cNb} := \frac{B_{cNb}}{\mu_0} \quad H_{cNb} = 1.432 \times 10^5 \frac{\text{A}}{\text{m}}$$

$$T_{cNb} := 9.2 \text{ K}$$

$$H_c(TT) := H_{cNb} \cdot \left[ 1 - \left( \frac{TT}{T_{cNb}} \right)^2 \right]$$

$$\mu_0 \cdot H_c(7.5 \text{ K}) = 60.376 \text{ mT}$$



# Results vs Model

- Future Tests
- New holder: better thermal contact between the copper and the superconducting sample.
- There is no thermal insulation between the cavity and the klystron. Only vacuum ~nTorr.
- Radiation heat?
- Low power test with the new holder with samples that did not become superconducting: single crystal Nb from Dessy.
- Future experiments will test very small pulses to avoid possible pulsed heating